

Mark Scheme (Results)

January 2021

Pearson Edexcel International GCSE Mathematics A (4MA1) Paper 1H

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.

Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.

- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

• Types of mark

- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

• Abbreviations

- cao correct answer only
- o ft follow through
- isw ignore subsequent working
- o SC special case
- oe or equivalent (and appropriate)

- dep dependent
- o indep independent
- awrt answer which rounds to
- eeoo each error or omission

• No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

• With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If there is a choice of methods shown, mark the method that leads to the answer on the answer line; where no answer is given on the answer line, award the lowest mark from the methods shown.

If there is no answer on the answer line then check the working for an obvious answer.

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

• Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

International (SCSE Maths				
	estions 5(b), 15, 17, 18, 19, 23 and 24 (where the		otherwise)	the corre	ect answer, unless clearly
-	incorrect method, should be taken to imply a co				
Q	Working	Answer	Mark		Notes
1	e.g. 0.7 × 20160 oe (= 14112)		4	M1	
	or 0.3 × 20160 oe (= 6048)				
	e.g. "14112" ÷ (9 + 5 + 2) (= 882)			M1	M2 for $9-2 \times 14112$ oe
	or (20160 - "6048") ÷ (9 + 5 + 2) (= 882)				$\frac{3}{9+5+2}$ × "14112" oe
	e.g. 9 × "882" – 2 × "882"			M1	
		6174		A1	
					Total 4 marks

2	(a)		$70 < s \le 80$	1	B1	
	(b)	$10 \times 45 + 16 \times 55 + 19 \times 65 + 23 \times 75 + 12 \times 85$	10 < 3 2 00	4	M2	$f \times d$ for at least 4 products with correct mid-interval values and
		or 450 + 880 + 1235 + 1725 + 1020 (= 5310)				intention to add.
						If not M2 then award M1
						for <i>d</i> used consistently for at least
						4 products within interval (including end points) and
						intention to add
						or
						for at least 4 correct products with
						correct mid-interval values with no intention to add
		"5310"÷80			M1	dep on at least M1 allow division
						by their $\sum f$ provided addition or
						total under column seen
			66.4		A1	accept 66.37 - 66.4
						Total 5 marks

3	e.g. $30 \times 20 \times 125$ (= 75 000) or $85 \times 40 \times 125$ (= 425 000) or $(60 \times 30 + (85 - 30) \times 40) \times 125$ (= 500 000) oe		4	M1	for a method to find the volume of water already pumped out or the volume of water left or the total volume of the container
	"75 000" ÷ 1.5 (= 50 000) or "75 000" ÷ 90 (= 833.3 or $\frac{2500}{3}$) or "425000" ÷ "75000" (= 5.66 or $\frac{17}{3}$) or "500000" ÷ "75000" (= 6.66 or $\frac{20}{3}$) "425 000" ÷ "50 000" (= 8.5) or "425 000" ÷ ("822.2.") × 60) op (= 8.5)			M1 M1	M2 for $\frac{"425000"}{"75000"} \times 1.5$ oe (= 8.5) or $\frac{"500000"}{"75000"} \times 1.5$ oe (= 10)
	or "425 000" ÷ ("833.3" × 60) oe (= 8.5) or "5.66" × 1.5 (= 8.5) or "6.66" × 1.5 (= 10)				
		20 30		A1	Allow 8 30 (pm)
					Total 4 marks

4 (i)	21, 27	1	B1
(ii)	21, 23, 24, 25, 27, 29	1	B1
			Total 2 marks

5 (a)		$5y^3(3y+4u)$	2	B2	for $5y^3(3y + 4u)$
				(B1	for $5y(3y^3 + 4uy^2)$ or $5y^2(3y^2 + 4uy)$ or $y^2(15y^2 + 20uy)$ or $y^3(15y + 20u)$ or $5y^3()$ where there is only one mistake in the brackets)
(b)	$4 \times (4-3x) = 5-8x \text{ oe}$ or $16-12x = 5-8x \text{ oe}$ or $4-3x = \frac{5}{4}-2x \text{ oe}$		3	M1	for removal of fraction in a correct equation
	e.g. $16-5=12x-8x$ or $11=4x$ oe or $4-\frac{5}{4}=3x-2x$			M1	for terms in x on one side and numbers on the other side in an equation, allow correct rearrangement of their equation in the form $ax + b = cx + d$
		2.75		A1	(dep on M1) oe e.g. $2\frac{3}{4}$ or $\frac{11}{4}$
					Total 5 marks

6	(a)	$2.84 imes 10^9$	1	B1
	(b)	0.000 25	1	B1
				Total 2 marks

7	(a)	for 0.035×40000 oe (= 1400) or 1.035×40000 oe (= 41400)	OR		3	M1	for finding 3.5% or 103.5% of 40000	OR M2 for 40000×1.035^3
		1.035 × "41 400" oe (= 42 849) 1.035 × "42 849" oe (= 44 348.72)	40000×1.035^3			M1	for completing method to find total amount in the account	or 40 000 × 1.035 ⁴ (= 45 900.92)
			1.033				the account	(M1 for 40000×1.035^2 (= 42 849))
				44 349		A1	accept 44 348 – 44 349	
							SC: if no other marks ga 0.105×40000 oe or 42 accept (1 + 0.035) as equilaterative throughout	00 or 44 200
	(b)	e.g. 30481 ÷ (1 − 0.065) or 30481 ÷	- 0.935		3	M2 (M1)	for a complete method for $30481 \div (100 - 6.5)$ or $(100 - 6.5)\% = 3048$ or e.g. $(1 - 0.065)x = 30$	1 or $93.5\% = 30481$
				32 600		A1		
								Total 6 marks

8	$2 \times \pi \times 7 (= 43.982 \text{ or } 14\pi)$ or $(2 \times \pi \times 7) \div 2 (= 21.991 \text{ or } 7\pi)$ or $2 \times \pi \times 9 (= 56.548 \text{ or } 18\pi)$ or $(2 \times \pi \times 9) \div 2 (= 28.274 \text{ or } 9\pi)$		3	M1	for finding the circumference of either the full circle or the length of the arc for either semicircle
	e.g. "21.991" + "28.274" (= 50.26) or " 7π " + " 9π " (=16 π) or "21.991" + "28.274" + 2 (= 52.26) or " 7π " + " 9π " + 2 (= 52.26) or "21.991" + "28.274" + 2 + 2 or " 7π " + " 9π " + 2 + 2			M1	for a method to find the length of the two arcs with intention to add
		54.3		A1	accept 54.2 – 54.3
					Total 3 marks

9	(a)		$16x^{12}y^{20}$	2	B2	B1 for an answer in the form
						$ax^n y^m$ with 2 correct from
						a = 16, n = 12, m = 20
	(b)(i)	$(x \pm 9)(x \pm 4)$		2	M1	for $(x \pm 9)(x \pm 4)$
						or for $(x + a)(x + b)$
						where $ab = -36$ or $a + b = 5$
			(x+9)(x-4)		A1	
	(ii)		-9, 4	1	B1	ft from (b)(i)
						Total 5 marks

10	e.g. $\sin 65 = \frac{16}{AB}$ or $\cos 25 = \frac{16}{AB}$ or $\frac{AB}{\sin 90} = \frac{16}{\sin 65}$ or $\tan 65 = \frac{16}{AD}$ or $\tan 25 = \frac{AD}{16}$ or $\frac{AD}{\sin 25} = \frac{16}{\sin 65}$		4	M1	for a correct trig ratio for <i>AB</i> or <i>AD</i> accept 180 – 90 – 65 for 25
	e.g. $(AB =) \frac{16}{\sin 65} (= 17.654)$ or $(AB =) \frac{16}{\cos 25} (= 17.654)$ or $(AB =) \frac{16\sin 90}{\sin 65} (= 17.654)$ and $(AD =) \frac{16}{\tan 65} (= 7.460)$ or $(AD) = 16 \times \tan 25 (= 7.460)$ or $(AD =) \frac{16\sin 25}{\sin 65} (= 7.460)$			M1	for finding <i>AB</i> and <i>AD</i> Allow use of Pythagoras $(AD =)\sqrt{17.654^2 - 16^2} (= 7.460)$ or $(AB =)\sqrt{7.460^2 + 16^2} (= 17.654)$
	$(``17.654" \times 2) + (``7.460" \times 2)$ oe			M1	for a complete method to find the perimeter
		50.2		A1	accept 49.6 – 50.6
					Total 4 marks

11 (a))			2	M1 for use of cf at 45
			146		A1 accept in the range $145 - 147$
(b))	93.75 ÷ 3.75 (= 25)		3	M1
		Using cf diagram at 90 – "25" (= 65)			M1 for use of cf at "65"
			151		A1 accept in the range $150 - 152$
					Total 5 marks

12 (a)	$\frac{4(x+1)-3(x-2)}{(x-2)(x+1)}$ or $\frac{4(x+1)}{(x-2)(x+1)} - \frac{3(x-2)}{(x-2)(x+1)}$		3	M1	for expressing both fractions correctly with a common denominator.
	$\frac{4x+4-3x+6}{(x-2)(x+1)} \text{ or } \frac{4x+4-3x+6}{x^2-x-2}$			M1	for removing brackets in a single fraction with a correct denominator. Allow denominator to be expanded. Allow one error in the expansion of the numerator.
		$\frac{x+10}{(x-2)(x+1)}$		A1	accept $\frac{x+10}{x^2-x-2}$ oe
(b)	$2x(x-5) = 2x^{2} - 10x$ or $2x(x-3) = 2x^{2} - 6x$ or $(x-5)(x-3) = x^{2} - 5x - 3x + 15(=x^{2} - 8x + 15)$		3	M1	for multiplying 2 <i>x</i> by a bracket with both terms correct or the 2 brackets with at least 3 out of 4 terms correct or at least 2 out of 3 terms correct
	$(2x^{2}-10x)(x-3) = 2x^{3}-6x^{2}-10x^{2}+30x$ or $(2x^{2}-6x)(x-5) = 2x^{3}-10x^{2}-6x^{2}+30x$ or $2x(x^{2}-5x-3x+15) = 2x^{3}-10x^{2}-6x^{2}+30x$ or $2x(x^{2}-8x+15) = 2x^{3}-16x^{2}+30x$			M1	(dep) for multiplying the product of $2x$ and the 1 st bracket (ft from the 1 st stage) by the 2 nd bracket and getting at least 3 out of 4 terms correct or multiplying the product of the 2 brackets (ft from the 1 st stage) by the 2 <i>x</i> , and getting at least 3 out of 4 or 2 out of 3 terms correct
		$2x^3 - 16x^2 + 30x$		A1	
					Total 6 marks

13 (a)	$\frac{84}{5-9} \left(= \frac{12}{-4} \right) \text{ oe or } \frac{-4-8}{9-5} \left(= \frac{-12}{4} \right) \text{ oe}$		2	M1 condone correct gradient embedded in an equation e.g. $y = -3x + c$ or expression e.g. $-3x$ or for an answer of 3
		-3		A1
(b)		$\frac{1}{4}$	1	B1 accept 0.25 or $-\frac{1}{-4}$ oe
				Total 3 marks

14 (a)	0.6 imes 0.9		2	M1 oe	
		0.54		A1 oe e.g. $\frac{27}{50}, \frac{54}{100}, 54\%$	
(b)	$0.6 \times 0.1 (= 0.06)$ or $0.4 \times 0.25 (= 0.1)$ or $0.4 \times 0.75 (= 0.3)$		3	M1 oe	
	$0.6 \times 0.1 + 0.4 \times 0.25$ or $1 - (0.4 \times 0.75) - 0.54$			M1 oe, ft their answer from	ı (a)
		0.16		A1 oe e.g. $\frac{4}{25}, \frac{8}{50}, \frac{16}{100}, 16$	5%
				Tot	tal 5 marks

15	9.55 or 9.65 or 3.75 or 3.85 or 1.835 or 1.845		3	B1	accept 9.649 for 9.65, 3.849 for 3.85, 1.8449 for 1.845
	$a = \frac{UB_v - LB_u}{LB_t}$ e.g. $a = \frac{9.65 - 3.75}{1.835} (= 3.2152)$			M1	for correct substitution of $9.6 < UB_v \square 9.65$ and $3.75 \square LB_u < 3.8$ and $1.835 \square LB_t < 1.84$
		3.22		A1	accept 3.21 – 3.22 from correct working
					Total 3 marks

16	$(BC^2 =)$ 150 ² + 275 ² - (2 × 150 × 275 × cos120) (= 139 375)		5 M1	for correct substitution into the cosine rule
	$(BC =) \sqrt{150^2 + 275^2 + 41250}$ oe or $\sqrt{139375}$		M1	
	or $25\sqrt{223}$ or 373			operations and square root
	e.g. $\frac{\sin ABC}{275} = \frac{\sin 120}{"373"}$		M1	(dep on 1 st M1) ft 373
				for a correct trig statement
	or $275^2 = 150^2 + "373"^2 - (2 \times 150 \times "373" \times \cos ABC)$			involving angle ABC
	or $\cos ABC = \frac{150^2 + "373"^2 - 275^2}{2 \times 150 \times "373"}$			or angle ACB
	or $\frac{\sin ACB}{150} = \frac{\sin 120}{"373"}$			
	or $150^{\circ} = 275^{\circ} + "373"^{\circ} - (2 \times 275 \times "373" \times \cos ACB)$			
	or $\cos ACB = \frac{275^2 + "373"^2 - 150^2}{2 \times 275 \times "373"}$			
	$(ABC =)\sin^{-1}\left(\frac{\sin 120}{"373"} \times 275\right) (= 39.6)$		M1	find angle ABC or angle
	or $(ABC =)\cos^{-1}\left(\frac{150^2 + "373"^2 - 275^2}{2 \times 150 \times "373"}\right) (= 39.6)$			ACB
	or $(ACB =) \sin^{-1} \left(\frac{\sin 120}{"373"} \times 150 \right) (= 20.3)$			
	or $(ACB =)\cos^{-1}\left(\frac{275^2 + "373"^2 - 150^2}{2 \times 275 \times "373"}\right) (= 20.3)$			
		140	A1	accept 140 – 140.4
				Total 5 marks

17	e.g. $(V =) \frac{1}{2} \left(\frac{4}{3} \pi x^3 \right) + \pi x^2 \left(20 - 4x \right)$ or $(V =) \frac{2}{3} \pi x^3 + 20 \pi x^2 - 4 \pi x^3$		5	M1	for a correct expression
	e.g. $\frac{1}{3}\pi y = \frac{1}{2}\left(\frac{4}{3}\pi x^3\right) + \pi x^2 (20 - 4x)$ or $\frac{1}{3}\pi y = \frac{2}{3}\pi x^3 + 20\pi x^2 - 4\pi x^3$			M1	for a correct equation
	$y = 60x^2 - 10x^3$ oe			A1	for writing <i>y</i> in terms of <i>x</i>
	e.g. $\left(\frac{\mathrm{d}y}{\mathrm{d}x}\right) = 120x - 30x^2 = 0$ oe			M1	for differentiating their $ax^2 + bx^3$ and equating to 0
		320		A1	(dep on M3) cao
					Total 5 marks

18	e.g. $40 + 8\sqrt{x} - 5\sqrt{x} - \sqrt{x}\sqrt{x}$ or $40 + 8\sqrt{x} - 5\sqrt{x} - (\sqrt{x})^2$ or $40 + 8\sqrt{x} - 5\sqrt{x} - x$ or $40 + 3\sqrt{x} - x$		3	M1	for a correct expansion with at least 3 out of 4 terms correct oe or all 3 terms correct
		<i>x</i> = 19		A1	(dep on M1) for $x = 19$
		<i>y</i> = 3		B1	for $y = 3$
					Total 3 marks

19	$(1-2y)^2 - 9y - (1-2y) = 2y^2 - 12$	$x^{2} - 9\left(\frac{1-x}{2}\right) - x = 2\left(\frac{1-x}{2}\right)^{2} - 12$		5	M1 substitution of linear equation into quadratic
	e.g. $2y^2 - 11y + 12(=0)$ oe allow $2y^2 - 11y = -12$ oe	e.g. $x^{2} + 9x + 14(=0)$ oe allow $x^{2} + 9x = -14$ oe			A1 (dep on M1) writing the correct quadratic expression in the form $ax^2 + bx + c (= 0)$
	e.g. $(2y-3)(y-4)(=0)$	e.g. $(x+7)(x+2)(=0)$			allow $ax^2 + bx = c$ M1 (dep on M1) for a complete method to solve their 3-term quadratic equation (allow one sign error and some
	$(y =) \frac{11 \pm \sqrt{(-11)^2 - 4 \times 2 \times 12}}{2 \times 2}$	$(x =) \frac{-9 \pm \sqrt{9^2 - 4 \times 1 \times 14}}{2}$			$\frac{11\pm\sqrt{121-72}}{4} \text{ or } \frac{-9\pm\sqrt{81-56}}{2} \text{)}$
	e.g. $2\left[\left(y - \frac{11}{4}\right)^2 - \left(\frac{11}{4}\right)^2\right] = -12$ oe	e.g. $\left(x + \frac{9}{2}\right)^2 - \left(\frac{9}{2}\right)^2 = -14$			
	$y = \frac{3}{2}$ oe and $y = 4$	x = -7 and $x = -2$			A1 (dep on M1) both <i>x</i> -values or both <i>y</i> -values
			x = -2, $y = \frac{3}{2} \text{ oe}$ and		A1 (dep on first M1) must be paired correctly
			x = -7, y = 4		
					Total 5 marks

20	$\sqrt[3]{\frac{4352}{1836}} \text{ or } \frac{4}{3} \text{ or } 1.33(33) \text{ or } 4:3$ or $\sqrt[3]{\frac{1836}{4352}} \text{ or } \frac{3}{4} \text{ or } 0.75 \text{ or } 3:4$ e.g. $1120 \div \left(\left\ \frac{4}{3} \right\ \right)^2$ oe or $1120 \times \left(\left\ \frac{3}{4} \right\ \right)^2$ oe		3	M1 M1	for a correct length scale factor or a correct length ratio (dep on M1) for a correct method
	e.g. $1120 \div \left(\frac{\pi}{3} \right)$ oe or $1120 \times \left(\frac{\pi}{4} \right)$ oe	(20		A 1	to work out the surface area of A
		630		A1	
					Total 3 marks

21	(a)(i)	(-12, 15)	1	B1
	(ii)	(-9, 5)	1	B1
	(b)	a = 2 and $b = 90$	2	B2 for both values correct (B1 for $a = 2$ or $b = 90$ or $a = -2$ and $b = -90$)
				Total 4 marks

22	$y = (x-4)^2 - 4^2 (+5)$ oe or $x = (y-4)^2 - 4^2 (+5)$		3	M1	for a correct first step in order to complete the square
	$y = 4 \pm \sqrt{11 + x}$ or $x = 4 \pm \sqrt{11 + y}$			A1	allow $y = 4 + \sqrt{11 + x}$ or $x = 4 + \sqrt{11 + y}$
		4- $\sqrt{x+11}$		A1	oe
					Total 3 marks

22 ALT	$x^{2} - 8x + (5 - y) = 0$ $(x =) \frac{8 \pm \sqrt{(-8)^{2} - 4 \times 1 \times (5 - y)}}{2 \times 1}$ or $y^{2} - 8y + (5 - x) = 0$ $(y =) \frac{8 \pm \sqrt{(-8)^{2} - 4 \times 1 \times (5 - x)}}{2 \times 1}$		3	M1 for a correct first step in preparation for use of quadratic formula and substitution into the quadratic formula (allow one sign error)
	$y = 4 \pm \sqrt{11 + x}$ or $x = 4 \pm \sqrt{11 + y}$			A1 allow $y = 4 + \sqrt{11 + x}$ or $x = 4 + \sqrt{11 + y}$
		4- $\sqrt{x+11}$		A1 oe
				Total 3 marks

22 ALT Using $ax^{2} + bx + c = a(x+p)^{2} + q$			
$\left(p = \frac{b}{2a}\right) = \frac{-8}{2}(=-4) \text{ and } q = (4)^2 - 8(4) + 5(=-11)$		3	M1 for finding p and q
$y = 4 \pm \sqrt{11 + x}$ or $x = 4 \pm \sqrt{11 + y}$			A1 allow $y = 4 + \sqrt{11 + x}$
			or $x = 4 + \sqrt{11 + y}$
	4- $\sqrt{x+11}$		A1 oe
			Total 3 marks

		г	<)	\longrightarrow \longrightarrow
23	$\overrightarrow{AB} = 2\mathbf{b} - 2\mathbf{a}$ oe or $\overrightarrow{BA} = 2\mathbf{a} - 2\mathbf{b}$ oe or $\overrightarrow{AM} = \mathbf{b} - \mathbf{a}$ oe or $\overrightarrow{MA} = \mathbf{a} - \mathbf{b}$ oe		6 M1	for finding \overrightarrow{AB} or \overrightarrow{BA} or
	or $\overline{BM} = \mathbf{b} - \mathbf{a}$ oe or $\overline{MB} = \mathbf{a} - \mathbf{b}$ oe			\overline{AM} or \overline{MA} or \overline{BM}
				or \overrightarrow{MB}
	e.g. $\overrightarrow{OM} = 2\mathbf{a} + (\mathbf{b} - \mathbf{a})(=\mathbf{a} + \mathbf{b})$ oe or $\overrightarrow{MO} = (\mathbf{b} - \mathbf{a}) - 2\mathbf{b}(=-\mathbf{a} - \mathbf{b})$ oe		M1	for finding \overrightarrow{OM} or \overrightarrow{MO}
	or $\overrightarrow{AN} = \frac{4}{3}\mathbf{b} - 2\mathbf{a}$ oe or $\overrightarrow{NA} = 2\mathbf{a} - \frac{4}{3}\mathbf{b}$ oe			or \overrightarrow{AN} or \overrightarrow{NA}
	e.g. $\overrightarrow{OP} = 2\mathbf{a} + \lambda \left(\frac{4}{3}\mathbf{b} - 2\mathbf{a}\right)$ oe or $\overrightarrow{OP} = \frac{4}{3}\mathbf{b} + \lambda \left(2\mathbf{a} - \frac{4}{3}\mathbf{b}\right)$ oe		M1	for finding \overrightarrow{OP} or \overrightarrow{PO} or \overrightarrow{MP} or \overrightarrow{PM}
	or $\overrightarrow{OP} = \mu(\mathbf{a} + \mathbf{b})$ oe OR $\overrightarrow{MP} = \mathbf{a} - \mathbf{b} + k\left(\frac{4}{3}\mathbf{b} - 2\mathbf{a}\right)$ oe			
	or $\overrightarrow{MP} = \mathbf{b} - \mathbf{a} - \frac{2}{3}\mathbf{b} + k\left(2\mathbf{a} - \frac{4}{3}\mathbf{b}\right)$ oe or $\overrightarrow{MP} = t\left(-\mathbf{a} - \mathbf{b}\right)$ oe			
	e.g. $2\mathbf{a} + \lambda \left(\frac{4}{3}\mathbf{b} - 2\mathbf{a}\right) = \mu \left(\mathbf{a} + \mathbf{b}\right)$ oe or $\frac{4}{3}\mathbf{b} + \lambda \left(2\mathbf{a} - \frac{4}{3}\mathbf{b}\right) = \mu \left(\mathbf{a} + \mathbf{b}\right)$ oe		M1	for setting up an equation for \overrightarrow{OP} or \overrightarrow{MP}
	or $\mathbf{a} - \mathbf{b} + k \left(\frac{4}{3}\mathbf{b} - 2\mathbf{a}\right) = t(-\mathbf{a} - \mathbf{b})$ oe or			
	$\mathbf{b} - \mathbf{a} - \frac{2}{3}\mathbf{b} + k\left(2\mathbf{a} - \frac{4}{3}\mathbf{b}\right) = t\left(-\mathbf{a} - \mathbf{b}\right)$ oe			
	4 1		M1	for finding μ or <i>t</i> for
	$\mu = \frac{4}{5}$ or $t = \frac{1}{5}$			either $\overrightarrow{OP} = \mu \overrightarrow{OM}$
				or $\overrightarrow{MP} = t \overrightarrow{MO}$
		4:1	A1	cao (dep on M3)
				Total 6 marks

24	$\frac{2n}{2} \left[2a + (2n-1)d \right] $ oe		4	M1	for a correct expression for S_{2n}
	$\left\lfloor \frac{2n}{2} \left[2a + (2n-1)d \right] = 4 \times \frac{n}{2} \left[2a + (n-1)d \right] \text{ oe} \right]$			M1	dep on M1 for setting up a correct equation for $S_{2n} = 4 \times S_n$
	2a - d = 4a - 2d oe			M1	for a correct linear expression in a and d
		$\frac{d}{2}$		A1	(dep on M2) for $\frac{d}{2}$ oe
					Total 4 marks

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