

LEVEL 2 CERTIFICATE FURTHER MATHEMATICS 8360/2

Paper 2 Calculator

Mark scheme

June 2019

Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M | Method marks are awarded for a correct method which could lead to a correct answer. |
|--------|--|
| M dep | A method mark dependent on a previous method mark being awarded. |
| A | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| В | Marks awarded independent of method. |
| B dep | A mark that can only be awarded if a previous independent mark has been awarded. |
| ft | Follow through marks. Marks awarded following a mistake in an earlier step. |
| sc | Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth. |
| oe | Or equivalent. Accept answers that are equivalent. |
| | eg, accept 0.5 as well as $\frac{1}{2}$ |
| [a, b] | Accept values between a and b inclusive. |
| 3.14 | Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416 |

Examiners should consistently apply the following principles.

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the candidate intended it to be a decimal point.

| Q | Answer | Mark | Comments | |
|------|--|------------|---|----------|
| | | | | |
| | Alternative method 1 | T | | |
| | 3a = 4(2a + 3) or $3a = 8a + 12$ | | oe equation | |
| | or | M1 | | |
| | 5a = 4b | | | |
| | $(a =) - \frac{12}{5}$ or $-2\frac{2}{5}$ or -2.4 | A1 | | |
| | (<i>b</i> =) –3 | | ft their $a \times 1.25$ evaluated | |
| | | A1ft | or $\frac{\text{their } 5a}{4}$ evaluated | |
| | | | $a \neq 0$ | |
| | | | if awarding ft M1 is implied | |
| | Alternative method 2 | T | | |
| | 3a + 5a = 4(2a + 3) + 4b | | oe equation | |
| | or $8a = 8a + 12 + 4b$ | M1 | | |
| 1(a) | or 4 <i>b</i> = –12 | | | |
| | (<i>b</i> =) –3 | A1 | | |
| | $(a =) - \frac{12}{5}$ or $-2\frac{2}{5}$ or -2.4 | | ft their $b \times 0.8$ evaluated | |
| | 5 5 | A1ft | or $\frac{\text{their } 4b}{5}$ evaluated | |
| | | 7,111 | <i>b</i> ≠ 0 | |
| | | | if awarding ft M1 is implied | |
| | Ad | ditional G | Buidance | |
| | Alt 1 | | | |
| | a = 2 $b = 2.5$ (5a = 4b is implied) | | | M1A0A1ft |
| | | | | МО |
| | Accept $\frac{-12}{5}$ or $\frac{12}{-5}$ for $-\frac{12}{5}$ (apply throughout scheme for values) | | | |
| | Only solutions seen with one correct and the other incorrect (or missing) | | | 2 marks |
| | | | | |

| Q | Answer | Mark | Comments | |
|--|--|------------|----------------------------|------|
| | | | | |
| | $2m + 2 = 1$ or $2m + 1 = 0$ or $\frac{1-2}{2}$ or $\begin{pmatrix} 2m+2 & 2m+1 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ | M1 | oe equation or calculation | |
| | $-\frac{1}{2}$ or -0.5 | | | |
| | Ad | ditional G | Buidance | |
| 1(b) | Condone missing brackets in $\begin{pmatrix} 2m+2 & 2m+1 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ | | | |
| | Allow $\begin{pmatrix} 2m+2 & 2m+1 \\ 2-2 & 2-1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ | | | |
| Mark positively eg error in matrix multiplication but $2m + 2 = 1$ and answer -0.5 | | | | M1A1 |
| | More than one answer given is A0 | | | |
| | eg $m+2=1$ and $2m+1=0$ (mark positively) | | M1 | |
| | Answer -1 and -0.5 | | | A0 |

| Q | Answer | Mark | Comments |
|---|---|------|---|
| | | | |
| | $\left(\frac{4+6}{2}, \frac{1+9}{2}\right)$ or (5, 6) | M1 | oe eg $\left(4 + \frac{6-4}{2}, 1 + \frac{11-1}{2}\right)$ may be on diagram |
| 2 | $\frac{13}{4-10}$ or $\frac{4}{-6}$ or $\frac{0-\text{their } 6}{14-\text{their } 5}$ or $\frac{-6}{9}$ | M1 | oe method for at least one gradient or at least one unsimplified gradient seen $eg \ \frac{-3-1}{10-4} \ or \ \frac{-4}{6}$ or $\frac{their \ 6-0}{their \ 5-14} \ or \ \frac{6}{-9}$ is M1M1 |
| | $\frac{13}{4-10} \text{ or } \frac{4}{-6}$ and $\frac{0-6}{14-5} \text{ or } \frac{-6}{9}$ and shows that the gradients are equal | A1 | oe method for both gradients or two unsimplified gradients seen and gradients shown to be equal $eg \ \frac{4}{-6} \ and \ \frac{-6}{9}$ and these are both $-\frac{2}{3}$ $SC2 \ (5, 6) \ and \ at \ least \ one \ gradient \ given \ as -\frac{2}{3} SC1 \ at \ least \ one \ gradient \ given \ as -\frac{2}{3}$ |

| Q | Answer | Mark | Comments |
|---|--------|------|----------|
|---|--------|------|----------|

| | Additional Guidance | | | | |
|-----------|--|----------|--|--|--|
| | Mark intention for 1st M1 eg condone 5, 6 | M1 | | | |
| | $\frac{4}{-6} = -\frac{2}{3}$ and $\frac{-6}{9} = -\frac{2}{3}$ | M2A1 | | | |
| | $\frac{13}{4-10} = -\frac{2}{3} \text{and} \frac{0-6}{14-5} = -\frac{2}{3}$ | M2A1 | | | |
| | $\frac{4}{-6} = \frac{-6}{9}$ | M2A1 | | | |
| | $\frac{4}{-6}$ and $\frac{-6}{9}$ and parallel | M2A0 | | | |
| | $\frac{4}{6}$ is 2nd M0 unless recovered to $-\frac{4}{6}$ | | | | |
| | $\frac{4}{6} \text{ recovered to } -\frac{4}{6} \text{ and } \frac{6}{9} \text{ recovered to } -\frac{6}{9} \text{ could go on to score full marks}$ $\text{both gradients } = -\frac{2}{3} \text{ with no method or unsimplified gradients seen cannot score the A mark}$ | | | | |
| 2 cont | | | | | |
| | $\frac{4}{-6}x$ or $\frac{-6}{9}x$ do not score 2nd M1 unless recovered | | | | |
| | Equation of a line does not score 2nd M1 unless a method or unsimplified gradient seen | | | | |
| | Using the reciprocals of gradients can score a maximum of M1M0A0 | | | | |
| | Allow -0.66 or -0.67 for $-\frac{2}{3}$ and $\frac{4}{-6}$ etc | | | | |
| | Ignore conversion attempt after a correct fraction is seen | | | | |
| | or method for $\frac{4}{-6}$ | | | | |
| | 1 = 4m + c and $-3 = 10m + c$ | | | | |
| | 4 = -6m | | | | |
| | $\frac{4}{-6} = m \qquad \text{(similar method possible for } \frac{-6}{9}\text{)}$ | (2nd) M1 | | | |

| Q | Answer | Mark | Comments | |
|---|--|-------------|----------------------------|--|
| | | | | |
| | $a^2 < 0$ | | B1 for each correct row | |
| | $-1 < b^3 < 1$ | D.4 | | |
| | $\frac{b}{a} < 0$ | B4 | | |
| | a-b>0 | | | |
| 3 | Additional Guidance | | | |
| | Two boxes ticked in a row with other 3 | correct B3 | | |
| | One row correct, two rows blank, all the | ree boxes | s ticked in another row B1 | |
| | Only crosses used instead of ticks | | | |
| | eg cross in all 4 correct boxes with all | s blank B4 | | |
| | Ticks and crosses used – only mark th | that row | | |
| | eg Top row has X X ✓ scores B1 t | V | | |
| | Second row has X ✓ X scores B0 for | or that row | | |

| Q | Answer | Mark | Comments |
|---|--|-------|---|
| | | | |
| | $(y =) \frac{3}{2}x$ or $(y =) 1.5x$ or $\frac{3}{2}$ or 1.5 | M1 | oe eg $(y =) \frac{3x - 9}{2}$ |
| | $\frac{x^5 - 17}{10} = \frac{3}{2}$ | M1dep | oe implies M2 |
| 4 | $x^5 = \frac{3}{2} \times 10 + 17$ or $\sqrt[5]{32}$ or correctly rearranges $\frac{x^5 - 17}{10} = k$ to the form $x^5 = (k \text{ any non-zero value})$ | M1 | oe eg $x^5 = 15 + 17$ or $x^5 = 32$ or $\sqrt[5]{15 + 17}$ must rearrange to the form $x^5 =$ |
| | 2 | A1 | |

| Q | Answer | Mark | Comments |
|---|--------|------|----------|
| , | | | |

| | Additional Guidance | |
|------|---|----------|
| | Condone error seen in rearrangement of $3x - 2y = 9$ if gradient is $\frac{3}{2}$ May go on to score M3A1 | |
| | $\frac{x^5 - 17}{10} = \frac{3}{2}x$ | M1M0M0A0 |
| | (gradient =) 3 | M0M0dep |
| | $\frac{x^5 - 17}{10} = 3$ | |
| 4 | $x^5 = 30 + 17$ (3rd M is not dependent) | M1 |
| cont | 2.16 | A0 |
| | $\frac{3}{2}$ | M1 |
| | $\frac{x^5 - 17}{10} = -\frac{2}{3}$ | MO |
| | $x^5 = -\frac{2}{3} \times 10 + 17$ (3rd M is not dependent) | M1 |
| | 1.595 | A0 |
| | Condone answer (2,) | |
| | 2 embedded | МЗАО |

| Q | Answer | Mark | Comments | |
|------|---|--------------|--|---|
| | | | | |
| 5(a) | a^{-2} | B2 | B1 applies an index law or changes root to fractional or decimal power in correct expression eg $ \sqrt[4]{a^{-8}} \text{or} (a^{-8})^{\frac{1}{4}} \text{or} (a^{8})^{-\frac{1}{4}} $ or $a^{-\frac{8}{4}} \text{or} \frac{1}{\frac{8}{a^{\frac{1}{4}}}} \text{or} \frac{1}{a^{\frac{2}{a}}}$ or $a^{\frac{1}{4}} \times a^{-\frac{9}{4}} \text{or} a^{\frac{1}{4}} \times \frac{1}{\frac{9}{a^{\frac{9}{4}}}}$ or $\left(\frac{1}{a^{8}}\right)^{\frac{1}{4}} \text{or} \sqrt[4]{\frac{1}{a^{\frac{8}{4}}}}$ or $\left(a \times a^{-9}\right)^{\frac{1}{4}} \text{or} \left(a \times \frac{1}{a^{\frac{9}{4}}}\right)^{\frac{1}{4}}$ | |
| | Ad | ditional G | Guidance | |
| | $a^{\frac{-8}{4}}$ or $a^{\frac{8}{-4}}$ | | В | 1 |
| | a^{-2} in working with -2 on answer line | | В | 1 |
| | a^{-2} in working with $\frac{1}{a^2}$ on answer line | | В | 1 |
| | B1 response followed by further work is | s still awar | ded B1 | |
| | Allow 0.25 for $\frac{1}{4}$ etc | | | |
| | Allow recovery of missing brackets | | | |

| Q | Answer | Mark | Comments | |
|------|--|--|--|--------------------------------|
| | | | | |
| | $32c^2d^2$ or $32(cd)^2$ | В3 | B2 (numerator =) $64c^3d^6$ or single term answer with two 32, c^2 and d^2 (not in a denor B1 single term answer with 32, c^2 and d^2 (not in a denor SC2 factorised correct express $16cd(2cd)$ | ninator) one of ninator) |
| | Ad | ditional G | Buidance | |
| | $2c^2d^2$ or $32c^2d$ or $32c^2$ or $\frac{32d^2}{c^3}$ | c^2 or $\frac{32d^2}{c^3}$ or $\frac{c^2d^2}{32}$ or $64(cd)^2$ etc | | B2 |
| 5(b) | $32c^3d$ or c^2 or $\frac{d^2}{c}$ or $\frac{c^2d}{32}$ or $\frac{32}{c^2}$ etc | | | B1 |
| | $\frac{32c^2d^2}{1}$ or $\frac{32(cd)^2}{1}$ | | | B2 |
| | Allow denominator of 1 in a B2 or B1 ar | nswer eg | $\frac{32c^2d}{1}$ | B2 |
| | Multiplication signs in a correct express | sion eg 32 | $2 \times c^2 \times d^2$ | B2 |
| | Allow multiplication signs in a B2, SC2 | Allow multiplication signs in a B2, SC2 or B1 answer eg $32 \times c^3 \times d$ | | |
| | Do not accept 2^5 for $32 - \operatorname{eg} 2^5 c^2 d$ | | | B1 |
| | If answer line scores B1 or B0 check working lines for possible response for up to 2 marks | | | |
| | $32c^2d^2$ in working with different answer | on answe | r line | B2 |

| Q | Answer | Mark | Comments |
|------|----------------------------------|--------------|---|
| | | | |
| | $A(-\frac{3}{2},0)$ and $B(2,0)$ | | ое |
| | 2 / / | B2 | B1 $A(-\frac{3}{2}, 0)$ oe or $B(2, 0)$ |
| 6(a) | | | 204 4(2.0) and D(3.0) as |
| 0(a) | | | SC1 $A(2, 0)$ and $B(-\frac{1}{2}, 0)$ oe |
| | | Additional G | uidance |
| | Ignore the diagram | | |
| 6(a) | Ignore the diagram | Additional G | SC1 $A(2, 0)$ and $B(-\frac{3}{2}, 0)$ or uidance |

| 6(b) | $-\frac{3}{2} < x < 2$ or $2 > x > -\frac{3}{2}$ | B1ft | oe correct or ft their values from (a) must be a single inequality in x |
|------|--|------|---|
|------|--|------|---|

| Q Answer | Mark | Comments |
|----------|------|----------|
|----------|------|----------|

| | Additional Guidance | | | | |
|--------------|--|------|--|--|--|
| | $-\frac{3}{2} \leqslant x < 2$ | В0 | | | |
| | $-\frac{3}{2} > x < 2$ | В0 | | | |
| | $-\frac{3}{2} < x$ and $x < 2$ | ВО | | | |
| | their (a) $A(-2, 0)$ and $B(\frac{3}{2}, 0)$ (B0 in (a)) | | | | |
| 6(b) cont | (b) $-2 < x < \frac{3}{2}$ | B1ft | | | |
| | their (a) $A(2,0)$ and $B(-\frac{3}{2},0)$ (SC1 in (a)) | | | | |
| | (b) $2 < x < -\frac{3}{2}$ | B0ft | | | |
| | their (a) $A(-3, 0)$ and $B(2, 0)$ (B1 in (a)) (b) $2 < x < -3$ | B0ft | | | |
| | their (a) A (4, 0) and B (-2, 0) (B0 in (a)) (b) $-2 < x < 4$ | B1ft | | | |
| | Only one value in (a) can only score in (b) for $-\frac{3}{2} < x < 2$ or $2 > x > -\frac{3}{2}$ | | | | |

| Q | Answer | Mark | Comments | 5 | |
|------|---|------------|----------------|----|--|
| | Horizontal straight line | B1 | mark intention | | |
| | Ac | ditional G | uidance | | |
| | Ignore any attempt at an equation | | | | |
| _, , | Mark the entire graph on the grid | | | | |
| 7(a) | Ignore any graph not on the grid | | | | |
| | Line clearly drawn on the x-axis | | | B1 | |
| | Line does not need to start from the y-axis | | | | |
| | Ignore any points plotted | | | | |
| | 1 | | 1 | | |
| | Straight line with gradient > 0 | B1 | mark intention | | |
| | Additional Guidance | | | | |
| | Ignore any attempt at an equation | | | | |
| | Mark the entire graph on the grid | | | | |

| | Straight line with gradient > 0 | B1 | mark intention | | |
|------|--|----|----------------|--|--|
| | Additional Guidance | | | | |
| | Ignore any attempt at an equation | | | | |
| | Mark the entire graph on the grid | | | | |
| 7(b) | Ignore any graph not on the grid | | | | |
| | Vertical line | | | | |
| | A straight line joined to another line with a different gradient | | | | |
| | Line does not need to start at (0, 0) | | | | |
| | Ignore any points plotted | | | | |

| Q | Answer | Mark | Comments | | |
|------|---|------|--|------|--|
| 8(a) | $7 + 12\sqrt{5} + 6(9 - 2\sqrt{5})$ or $12\sqrt{5} + 6(-2\sqrt{5}) = 0$ or $12\sqrt{5} \div 2\sqrt{5} = 6$ or states that need to add 6 lots of $(9 - 2\sqrt{5})$ or $7th term$ | M1 | oe eg $7 + 6 \times 9$ or $7 + 54$ or $6 \times -2 = -12$ allow $7 + 12\sqrt{5} + (n-1)(9 - 2\sqrt{5})$ with $n = 7$ allow $7 + 12\sqrt{5} + n(9 - 2\sqrt{5})$ with $n = 6$ | | |
| | 61 | A1 | | | |
| | Additional Guidance | | | | |
| | 61 in working lines with 7(th) on answer line | | | M1A0 | |
| | If repeatedly adding $(9-2\sqrt{5})$ they must stop after adding 6 lots or clearly select the relevant one | | | | |
| | Answer 6 or 6th term with M1 not seen | | | M0A0 | |
| | Ignore any conversions to decimals | | | | |
| | Beware $(9-2\sqrt{5})(9+2\sqrt{5}) = 61$ | | | M0A0 | |

| Q | Answer | Mark | Comments | 3 |
|------|---|------|---|-----------|
| | $\frac{29}{5}$ or $5\frac{4}{5}$ or 5.8 | B2 | oe eg $5\frac{8}{10}$ B1 any two of 1, $\frac{11}{5}$, $\frac{26}{10}$ | oe values |
| | Additional Guidance | | | |
| 8(b) | Terms must be evaluated for B1 unless correct answer seen | | | |
| O(B) | eg1 $\frac{3-1}{1+1} + \frac{12-1}{4+1} + \frac{27-1}{9+1}$ | | | В0 |
| | eg2 $\frac{3-1}{1+1} + \frac{12-1}{4+1} + \frac{27-1}{9+1} = 5.8$ | | | B2 |
| | 1 7 2.6 | | | B1 |
| | Ignore conversion attempts after a correct value seen | | | |

| Q | Answer | Mark | Comments | | |
|------|---|-------|--|--|--|
| | Alternative method 1 | | | | |
| | (Second differences =) 4 or $2n^2$ | M1 | second differences seen at least once and not contradicted may be seen by the sequence | | |
| | -3 - 2 3 - 8 (13 - 18 27 - 32) or -5 -5 (-5 -5) | M1dep | subtracts $2n^2$ from the given terms | | |
| | $2n^2 - 5$ | A1 | oe eg $2n^2 + 0n - 5$ does not need terms collected | | |
| 8(c) | Alternative method 2 | | | | |
| | (Second differences =) 4 or $2n^2$ | M1 | second differences seen at least once and not contradicted | | |
| | | | may be seen by the sequence | | |
| | 3a + b = 33 and substitutes $a = 2$ or $b = 0$ | M1dep | oe | | |
| | $2n^2 - 5$ | A1 | oe eg $2n^2 + 0n - 5$ does not need terms collected | | |

| Q | Answer | Mark | Comments | | |
|--------------|--|-------|--|------|--|
| | Alternative method 3 | | | | |
| | Any three of $a + b + c = -3$ 4a + 2b + c = 3 9a + 3b + c = 13 16a + 4b + c = 27 | M1 | | | |
| | 3a + b = 33 and $5a + b = 13 - 3$ or a = 2 and $b = 0$ | M1dep | oe obtains two correct equations in same two variables from their equations | | |
| | $2n^2-5$ | A1 | oe eg $2n^2 + 0n - 5$ does not need terms collected | | |
| | Alternative method 4 | | | | |
| 8(c) cont | (Second differences =) 4 or $2n^2$ | M1 | second differences seen at least once and not contradicted may be seen by the sequence | | |
| | $2 \times 1^{2} + b \times 1 - 5 = -3$ or $2 + b - 5 = -3$ or $b = 0$ | M1dep | $2n^{2} + bn - 5 = -3 \text{ with } n = 1 \text{ substituted}$ oe $eg \ 2 \times 2^{2} + b \times 2 - 5 = 3$ | | |
| | $2n^2 - 5$ | A1 | oe eg $2n^2 + 0n - 5$ does not need terms collected | | |
| | Additional Guidance | | | | |
| | Condone working in a different variable | | | | |
| | Alt 1 2nd M1 Subtracting given terms from $2n^2$ leading to 5 5 (5 5) must be recovered eg final answer $2n^2 - 5$ $(2n^2 - 5n \text{ or } 2n^2 - 5n - 5 \text{ is not a recovery})$ | | | | |
| | Answer $2n^2$ scores at least M1 | | | | |
| | Condone $n = 2n^2 - 5$ or $2n^2 - 5 = 0$ | | | M2A1 | |

| 1) and $x^{10}(x-1)$ |
|--|
| r than p) isation $-(p+6)^{9}$ $-(p+6)^{8}$ |
| |
| |
| B1 |
| В0 |
| B2 |
| B1 |
| i |

| Q | Answer | Mark | Comments | | |
|-------|---|-------------|--|-----|--|
| | $f(x) \le 25$ or $25 \ge f(x)$ | B2 | B1 $f(x) < 25$ or $k \le f(x) \le 25$ or $k < f(x) \le 25$ where k is any number < 25 SC1 ≤ 25 or $x \le 25$ | 5 | |
| | | Iditional G | | | |
| | Condone $f(x)$ replaced by eg y or f or $f(x)$ or | | | | |
| | Equivalent inequalities may be seen | | | | |
| | 25 > f(x) | | | B1 | |
| 10(a) | Allow $-\infty < f(x) \le 25$ | | | B2 | |
| | Condone $-\infty \le f(x) \le 25$ | | | B2 | |
| | $-\infty < f(x) < 25$ or $-\infty \leqslant f(x) < 25$ | | | B1 | |
| | $[-\infty, 25]$ or $(-\infty, 25]$ | | | B1 | |
| | (–∞, 25) | | | В0 | |
| | Condone $f(x) = \leq 25$ | | | B2 | |
| | Condone $f(x) = \langle 25 \rangle$ | | | B1 | |
| | Condone $f(x) = x \le 25$ | | | SC1 | |
| | $f(x) \le 25$ in working with list of integers on answer line | | | B1 | |
| | Only a list of integers | | | В0 | |

| Q | Answer | Mark | Comments | |
|-------|--|----------------------|--|----------|
| | $1 \leqslant g(x) \leqslant 5$ or $5 \geqslant g(x) \geqslant 1$ | B2 | B1 $1 \le g(x) < 5$ or $1 < g(x)$ or $1 < g(x) < 5$ or $1 < g(x) < 5$ or $g(x) \ge 1$ and $g(x) \le 5$ or $1 \le g(x) \le k$ where k is a constant > 1 or $p \le g(x) \le 5$ where p is a constant < 5 SC1 $1 \le x \le 5$ | x) ≤ 5 |
| | Ac | Iditional G | uidance | |
| | Condone $g(x)$ replaced by eg y or g or g in B2 or B1 responses | f or fx or $5 - x^2$ | | |
| | Equivalent inequalities may be seen | eg 5 ≥ g(x | s) > 1 | B1 |
| 10(b) | Only $g(x) \ge 1$ given as the answer | | | В0 |
| | Only $g(x) \le 5$ given as the answer | | | В0 |
| | $1 \leqslant g(x) \leqslant 4$ | | | B1 |
| | $1 \leqslant g(x) < 4$ | | | В0 |
| | $0 \leqslant g(x) \leqslant 5$ | | | B1 |
| | $0 < g(x) \leqslant 5$ | | | В0 |
| | Invalid statements do not score | | | |
| | eg1 $1 \leqslant g(x) \geqslant 5$ | | | B0 |
| | $eg2 1 \geqslant g(x) \leqslant 5$ | | | B0 B0 |
| | eg3 $6 \leqslant g(x) \leqslant 5$ | | | |
| | [1, 5] | | | B1 |
| | [1, 5) or (1, 5] or (1, 5) or 1 – 5 or 8 | | | B0 |
| | $1 \leqslant g(x) \leqslant 5$ in working with list of integration | gers on ans | wer line | B1 |
| | Only a list of integers | | | В0 |

| Q | Answer | Mark | Comments |
|----|---|------|---|
| | x = -2 | B1 | |
| 11 | Additional Guidance | | |
| | | | |
| | Alternative method 1 | | |
| | $\frac{1}{2} \times \frac{4}{3} \times \pi \times (6a)^3$ | | oe eg $\frac{1}{2} \times \frac{4}{3} \times \pi \times \left(\frac{12a}{2}\right)^3$ |
| | or $\frac{2}{3} \times \pi \times 216a^3$ | M1 | or $\frac{2}{3} \times \pi \times (6a)^3$ |
| | or 144π a^3 | | |
| 12 | $a^3 = \frac{486\pi}{144\pi}$ or $a^3 = \frac{27}{8}$ | | oe equation of form a^3 = or calculation allow $(6a)^3$ = 729 or $6a$ = 9 |
| | or $a^3 = 486 \div \left(\frac{2}{3} \times 6^3\right)$ | A1 | |
| | or $a^3 = 3.375$ | | |

Α1

SC1 answer 0.75 oe

or answer 1.19... or answer 4.95...

or $\sqrt[3]{3.375}$

 $\frac{3}{2}$ or $1\frac{1}{2}$ or 1.5

| Q | Answer | Mark | Comments | | |
|------------|--|--------------------------|--|--|--|
| | Alternative method 2 | | | | |
| | $r^{3} = \frac{486\pi}{\frac{2}{3}\pi}$ or $r^{3} = 729$ or $\sqrt[3]{729}$ or 9 | M1 | oe equation of form $r^3 =$ or calculation | | |
| 12 cont | $6a = \sqrt[3]{\frac{486\pi}{\frac{2}{3}\pi}}$ or $6a = 9$ or $9 \div 6$ | A1 | oe equation or calculation allow $(6a)^3 = 729$ | | |
| | $\frac{3}{2}$ or $1\frac{1}{2}$ or 1.5 | or $1\frac{1}{2}$ or 1.5 | SC1 answer 0.75 oe or answer 1.19 or answer 4.95 | | |
| | Ad | uidance | | | |
| | Allow recovery of missing brackets | | | | |
| | Allow use of $\pi = [3.14, 3.142]$ | | | | |

| Q | Answer | Mark | Comments | |
|----|---|-------------|---|------------------|
| | $x(1-x^2)$ or $2x(1+x)$ or $x(2+2x)$ or $\frac{1-x^2}{2+2x}$ | M1 | implied by 2nd M1 oe factorisation eg $-x(x^2 - 1)$ | |
| | $x(1+x)(1-x)$ or $\frac{x(1-x^2)}{2x(1+x)}$ or $\frac{1-x^2}{2(1+x)}$ or $\frac{(1+x)(1-x)}{2+2x}$ | M1dep | implies M2 oe factorisation eg $-x(x + 1)(x - 1)$ | |
| 13 | $\frac{x(1+x)(1-x)}{2x(1+x)}$ or $\frac{(1+x)(1-x)}{2(1+x)}$ or $\frac{x(1-x)}{2x}$ | M1dep | implies M3 oe factorisation $eg \frac{-x(x+1)(x-1)}{2x(1+x)}$ | |
| | $\frac{1-x}{2}$ with M3 seen | A1 | oe simplest form $eg \frac{1}{2}(1-x) \text{ or } \frac{1}{2} - \frac{1}{2}x \text{ or }$ | $\frac{-x+1}{2}$ |
| | Ac | lditional G | uidance | |
| | $\frac{x(1+x)(1-x)}{2x(1+x)} \text{ or } \frac{(1+x)(1-x)}{2(1+x)} \text{ or } \frac{x(1-x)}{2x}$ is sufficient working | | | M3 |
| | $2(x + x^2)$ with no further work | | | MO |
| | $\frac{x-1}{-2}$ with M3 seen or $-\frac{1}{2}(x-1)$ with M3 seen or $\frac{-(x-1)}{2}$ with M3 seen | | | M3A1 |

| Q | Answer | Mark | Comments | |
|----|---|------------|---|--------|
| | | | | |
| | $a^{2} + (3a)^{2} - 2 \times a \times 3a \times \cos 120$ or $\cos 120 = \frac{a^{2} + (3a)^{2} - b^{2}}{2 \times a \times 3a}$ | M1 | oe eg may substitute cos 1: may be seen in a square roo | |
| | $b^{2} = a^{2} + 9a^{2} + 3a^{2}$ or $b^{2} = 13a^{2}$ or $-b^{2} = -13a^{2}$ or $b = \sqrt{13} a$ | A1 | oe equation of the form $b^2 = \text{ or } b = \text{ with brackets expanded and terms fully simplified}$ $\cos 120 = -0.5 \text{ substituted}$ | |
| 14 | 13:1 | A1 | SC1 7:1 | |
| | Ad | ditional G | uidance | |
| | Allow recovery of missing brackets | | | |
| | $a^2 = a^2 + (3a)^2 - 2 \times a \times 3a \times \cos 120$ not recovered | | | M1M0A0 |
| | $b^2 = 10a^2 - 3a^2$ | | | M1A0A0 |
| | $b^2 = 10a^2 + 3a^2$ | | | M1A1A0 |

| Q | Answer | Mark | Comments |
|----|---|-------|---|
| | Alternative method 1 | | |
| | $3mp = 3(2p+1) + p + 5$ or $(m =) \frac{3(2p+1)}{3p} + \frac{p+5}{3p}$ or $(m =) \frac{6p+3+p+5}{3p}$ | M1 | oe fractions eliminated or common denominator $eg (m =) \frac{3p(2p+1)}{3p^2} + \frac{p(p+5)}{3p^2}$ or $(m =) \frac{6p^2 + 3p + p^2 + 5p}{3p^2}$ |
| 15 | 3mp = 6p + 3 + p + 5 or $3mp = 7p + 8$ | M1dep | oe brackets expanded and fractions eliminated eg $3mp^2 = 7p^2 + 8p$ implies M2 |
| | 3mp - 7p = 8 or $\frac{8}{3m - 7}$ or $\frac{-8}{7 - 3m}$ | M1dep | oe terms collected $eg \ p(3m-7) = 8 \ or \ 7p - 3mp = -8$ implies M3 |
| | $p = \frac{8}{3m - 7}$ or $p = \frac{-8}{7 - 3m}$ | A1 | oe eg $\frac{8}{3m-7} = p$ |

| Q | Answer | Mark | Comments |
|------------|---|-------------|--|
| | Alternative method 2 | | |
| | $(m =) \frac{3(2p+1)}{3p} + \frac{p+5}{3p}$ or $(m =) \frac{6p+3+p+5}{3p}$ | M1 | oe common denominator eg $(m =) \frac{3p(2p+1)}{3p^2} + \frac{p(p+5)}{3p^2}$ or $(m =) \frac{6p^2 + 3p + p^2 + 5p}{3p^2}$ |
| | $m = \frac{7p + 8}{3p}$ and $m = \frac{7}{3} + \frac{8}{3p}$ and $m - \frac{7}{3} = \frac{8}{3p}$ | M1dep | simplifies numerator and isolates term in p eg $m = \frac{7p^2 + 8p}{3p^2}$ and $m = \frac{7}{3} + \frac{8}{3p}$ and $m - \frac{7}{3} = \frac{8}{3p}$ implies M2 |
| 15 cont | $\frac{3m-7}{3} = \frac{8}{3p}$ | M1dep | converts $m - \frac{7}{3}$ to a single fraction implies M3 |
| | $p = \frac{8}{3m - 7}$ or $p = \frac{-8}{7 - 3m}$ | A1 | $oe eg \frac{8}{3m-7} = p$ |
| | Ac | Iditional G | uidance |
| | $p = \frac{8}{3m - 7}$ in working but $\frac{8}{3m - 7}$ on a | nswer line | M3A1 |
| | Allow recovery of missing brackets | | |
| | $p = \frac{8}{3m - 7}$ followed by incorrect further | | МЗАО |
| | Allow equivalences for A1 eg $p = \frac{\frac{8}{3}}{\frac{3m-3}{3}}$ | M3A1 | |
| | Do not regard eg $3m(p) = 7p + 8$ as h | aving unexp | panded brackets M1M1dep |

| Q | Answer | Mark | Comments | |
|----|--|-------|---|----|
| | | | | |
| | $\frac{8-5}{2} = \sqrt{1-a} \text{ or } \frac{3}{2} = \sqrt{1-a}$ or $3^2 = 2^2(1-a) \text{ or } 9 = 4(1-a)$ | M1 | | |
| 16 | $1 - a = \left(\frac{3}{2}\right)^2$ or $1 - a = \frac{9}{4}$ or $9 = 4 - 4a$ or $\frac{4 - 9}{4}$ | M1dep | oe equation or calculation $eg \ 1 - a = \left(\frac{8 - 5}{2}\right)^{2}$ or $1 - a = 2.25$ or $\frac{9 - 4}{-4}$ implies M2 | |
| | $-\frac{5}{4}$ or -1.25 or $-1\frac{1}{4}$ | A1 | | |
| | Additional Guidance | | | |
| | $3 = 2\sqrt{1 - a}$ | | | MO |
| | Allow recovery of missing brackets | | | |

| Q | Answer | Mark | Comments |
|----|--|-------|---|
| | $x^2 + 3x + x + 3$ with three terms correct or $x^2 + 4x + k$ where k is a non-zero constant | M1 | oe expansion attempt of one pair of brackets eg1 $x^2 + 4x + 3x + 12$ with three terms correct or $x^2 + 7x + k$ where k is a non-zero constant eg2 $x^2 + 4x + x + 4$ with three terms correct or $x^2 + 5x + k$ where k is a non-zero constant |
| 17 | $x^{3} + 3x^{2} + x^{2} + 3x$ or $x^{3} + 4x^{2} + 3x$ or $4x^{2} + 12x + 4x + 12$ or $4x^{2} + 16x + 12$ | M1dep | attempt at a full expansion with correct multiplication of their 3 or 4 terms by one of the terms in the remaining bracket oe eg $x^3 + 4x^2 + 3x^2 + 12x \text{ or } x^3 + 7x^2 + 12x$ or $x^2 + 4x + 3x + 12$ or $x^2 + 7x + 12$ $(x^2 + 7x + 12 \text{ must be from an attempt at a full expansion})$ or $x^3 + 4x^2 + x^2 + 4x \text{ or } x^3 + 5x^2 + 4x$ or $3x^2 + 12x + 3x + 12$ or $3x^2 + 15x + 12$ |
| | $x^3 + 8x^2 + 19x + 12$ | A1 | fully correct expansion allow if terms not collected eg $x^3 + 3x^2 + x^2 + 3x + 4x^2 + 12x + 4x + 12$ or $x^3 + 4x^2 + 3x + 4x^2 + 16x + 12$ |
| | $x^2 + 8x + 12$ | A1ft | ft M2A0 full simplification of their $(x^3 + 8x^2 + 19x + 12) - x^3 - 7x^2 - 11x$ their $(x^3 + 8x^2 + 19x + 12)$ must be a cubic |
| | $x^{2} + 8x + 12$ and (x + 6)(x + 2) or $(x + 2)(x + 6)$ | A1 | oe product of brackets |

| Q | Answer | Mark | Comments |
|---|--------|------|----------|
| | | | |

| | Additional Guidance | |
|------------|--|--------|
| | 1st M1 Do not allow omissions or extras | |
| | eg1 $x^2 + 3x + 3$ | MO |
| | eg2 $x^2 + 3x + x + 3 + x^2$ | MO |
| | For the first 2 marks terms may be seen in a grid | |
| | If 1st A1 has been awarded with terms not collected, A1ft can still be awarded using their simplified cubic | |
| | eg $x^3 + 4x^2 + 3x + 4x^2 + 16x + 12$ | M1M1A1 |
| | $= x^3 + 8x^2 + 18x + 12$ | |
| | $x^3 + 8x^2 + 18x + 12 - x^3 - 7x^2 - 11x$ | |
| 17 cont | $=x^2 + 7x + 12$ | A1ftA0 |
| | First A1 may be seen embedded | |
| | eg $x^3 + 8x^2 + 19x + 12 - x^3 + 7x^2 - 11x$ | M1M1A1 |
| | If an attempt at the expansion of all three brackets in one go is made it must be fully correct to gain M2A1, otherwise M0M0A0 | |
| | eg $x^2 + 3x + x + 3 + x^2 + 4x$ | M0M0A0 |
| | Allow recovery of missing brackets when subtracting $x^3 + 7x^2 + 11x$ from their cubic | |
| | For final A1 allow $x^2 + 8x + 12$ and $a = 6$ $b = 2$ | |
| | or $x^2 + 8x + 12$ and $a = 2$ $b = 6$ | |
| | Ignore equating to zero and/or any 'solving' of an equation | |

| Q | Answer | Mark | Comments | |
|----|---|------------|---|--|
| | Alternative method 1 | | | |
| | $x-5 = \frac{k}{2}$ or $x-5 = -\frac{k}{2}$ or $2(x-5) = k$ or $2x - 10 = k$ or $2(x-5) = -k$ or $2x - 10 = -k$ | M1 | oe linear equation $eg \ x - 5 = \sqrt{\frac{k^2}{4}} or \ x = \frac{k}{2} + 5$ or $\sqrt{4}(x - 5) = \sqrt{k^2}$ | |
| | $x-5 = \frac{k}{2}$ and $x-5 = -\frac{k}{2}$ or 2(x-5) = k and $2(x-5) = -kor2x-10 = k$ and $2x-10 = -k$ | A1 | oe eg $x - 5 = \pm \frac{k}{2}$ square root(s) must be processed implied by final A1 | |
| 18 | $\frac{k}{2}$ +5 and $-\frac{k}{2}$ +5 | A1 | oe simplest form $eg \ \frac{10+k}{2} \ and \ \frac{10-k}{2}$ or $\frac{k+10}{2}$ and $\frac{k-10}{-2}$ or $5 \pm 0.5k$ | |
| | Alternative method 2 | | | |
| | $4x^2 - 40x + 100 - k^2 (= 0)$ | M1 | expands and collects terms | |
| | $\frac{40 \pm \sqrt{(-40)^2 - 4 \times 4 \times (100 - k^2)}}{2 \times 4}$ | A1 | oe eg $\frac{40 \pm \sqrt{16k^2}}{8}$ or $\frac{40 \pm 4k}{8}$ implied by final A1 | |
| | $\frac{k}{2}$ +5 and $-\frac{k}{2}$ +5 | A1 | oe simplest form $eg \ \frac{10+k}{2} \ and \ \frac{10-k}{2}$ or $\frac{k+10}{2}$ and $\frac{k-10}{-2}$ or $5 \pm 0.5k$ | |
| | Ad | ditional G | uidance | |
| | Allow recovery of missing brackets | | | |

| Q | Answer | Mark | Comments | |
|-------|--|------|---|----|
| 19(a) | $\sqrt{(3x)^2 + (4x)^2} = (5x)$ or $\sqrt{9x^2 + 16x^2} = (5x)$ or $(3x)^2 + (4x)^2 = (5x)^2$ or $3x, 4x, 5x \text{ triangle}$ | B1 | may be seen in stages eg $9x^2 + 16x^2 = 25x^2$ and $\sqrt{25x^2}$ (= 5x) | |
| | Additional Guidance | | | В0 |
| | Only $\sqrt{25x^2}$ (= 5x) seen Pythagorean triple 3x, 4x, 5x | | | В1 |
| | Pythagorean triple 3, 4, 5 | | | B0 |
| | Missing brackets can not be recovered | | | |
| | eg1 $\sqrt{3x^2 + 4x^2} = 5x$ | | | В0 |
| | eg2 $3x^2 + 4x^2 = 9x^2 + 16x^2 = 25x^2$ and $\sqrt{25x^2}$ (= 5x) | | | В0 |
| | Incorrect statements are B0 (mark the f | | | |
| | eg1 $9x^2 + 16x^2 = 25x^2 = \sqrt{25x^2}$ (= 5x) | | | В0 |
| | eg2 $9x^2 + 16x^2 = 25x^2$ $\sqrt{25}x^2 = 5x$ | | | В0 |
| | eg3 $\sqrt{(3x)^2 + (4x)^2} = 5x$ and $3x + 4x = 5x$ | | | В0 |
| | Only uses values for x | | | В0 |

| | Mark | Comments | | | | | |
|---|--|---|--|--|--|--|--|
| Alternative method 1 | | | | | | | |
| $4x \times 3x \text{ or } 6x^2$ | M1 | oe may be seen on the diagram | | | | | |
| $(2.5x)^{2} - (2.5x)^{2}$ $(2.25x^{2} - 6.25x^{2})$ $(2.25x^{2} - 6.25x^{2})$ | M1 | oe eg $(6.5x)^2 - \left(\frac{5x}{2}\right)^2$ | | | | | |
| $\frac{1}{x^2} = \frac{1}{x^2} - \frac{1}{x^2}$ | M1dep | dep on 2nd M1 may be seen on the diagram | | | | | |
| $5x \times \text{their } 6x \text{ or } 15x^2$ | M1dep | oe dep on 2nd and 3rd M1 | | | | | |
| 2 | A1 | allow $p = 21$ if areas $6x^2$ and $15x^2$ seen | | | | | |
| Alternative method 2 | | | | | | | |
| $4x \times 3x \text{ or } 6x^2$ | M1 | oe may be seen on the diagram | | | | | |
| $ACD = \frac{2.5x}{6.5x}$ $\cos ACD = \frac{5}{13}$ | M1 | oe | | | | | |
| $\frac{2.5x}{6.5x}$ 7(.3) or 67.4 | M1dep | oe $eg cos^{-1} \frac{(6.5x)^2 + (5x)^2 - (6.5x)^2}{2 \times 6.5x \times 5x}$ | | | | | |
| | | dep on 2nd M1 | | | | | |
| $5x \times 6.5x \times \sin \text{ their } 67(.3)$ | M1dep on 2nd and 3rd M1 | | | | | | |
| 2 | A1 | allow $p = 21$ if areas $6x^2$ and $15x^2$ seen | | | | | |
| | $0^{2} - (2.5x)^{2}$ $2.25x^{2} - 6.25x^{2}$ $5x^{2}$ $5x \times \text{their } 6x \text{ or } 15x^{2}$ native method 2 $4x \times 3x \text{ or } 6x^{2}$ $ACD = \frac{2.5x}{6.5x}$ $ACD = \frac{5}{13}$ $1 \frac{2.5x}{6.5x}$ $7(.3) \text{ or } 67.4$ $5x \times 6.5x \times \text{ sin their } 67(.3)$ | $4x \times 3x \text{ or } 6x^2$ $y^2 - (2.5x)^2$ $2.25x^2 - 6.25x^2$ $3x^2$ M1 $5x^2$ M1 M1 M1 M1 M1 M1 M1 M1 M1 M | | | | | |

| Q | Answer | Mark | Comments | | | | |
|---------------|--|---------|---|--|--|--|--|
| | Alternative method 3 | | | | | | |
| - | $0.5 \times 4x \times 3x$ or $6x^2$ | M1 | oe may be seen on the diagram | | | | |
| | $(5x)^2 = (6.5x)^2 + (6.5x)^2$ $-2 \times 6.5x \times 6.5x \times \cos D$ | M1 | oe | | | | |
| | $\cos^{-1} \frac{(6.5x)^2 + (6.5x)^2 - (5x)^2}{2 \times 6.5x \times 6.5x}$ | | oe dep on 2nd M1 | | | | |
| | or $\cos^{-1} \frac{119}{169}$ | M1dep | | | | | |
| | or 45(.2) | | | | | | |
| | $0.5 \times 6.5x \times 6.5x \times \text{sin their } 45(.2)$ or $15x^2$ | M1dep | oe dep on 2nd and 3rd M1 | | | | |
| 19(b) cont | 21 <i>x</i> ² | A1 | allow $p = 21$ if areas $6x^2$ and $15x^2$ seen | | | | |
| | Additional Guidance | | | | | | |
| | Allow recovery of algebra eg1 $0.5 \times 4 \times 3 = 6$ is 1st M0 but if reco | | | | | | |
| | eg2 Alt 1 $\sqrt{42.25}$ - 6.25 = 6 is 2nd M0 6x scores 2nd M1 and 3rd M1 | | | | | | |
| | Do not allow final mark if an incorrect a eg do not allow answer $21x^2$ if their two | | | | | | |
| | Answer $21x^2$ with no incorrect working eg fully correct working with numbers a | 5 marks | | | | | |
| | Allow recovery of missing brackets | | | | | | |
| | Choose the scheme that favours the str | | | | | | |
| | eg1 $0.5 \times 4 \times 3 = 6$ is 1st M0 but if recovery eg2 Alt 1 $\sqrt{42.25 - 6.25} = 6$ is 2nd M0 $6x$ scores 2nd M1 and 3rd M1 Do not allow final mark if an incorrect a eg do not allow answer $21x^2$ if their two Answer $21x^2$ with no incorrect working eg fully correct working with numbers a Allow recovery of missing brackets | 5 ma | | | | | |

| Q | Answer | Mark | Comments |
|-------|--|---------------------|--|
| | Alternative method 1 | | |
| | Full method leading to angle $BCD = 180 - 2x$ | M1 | eg angle $CFE = x$ and angle $FCE = 180 - 2x$ and angle $BCD = 180 - 2x$ |
| | Full reasoning for their method | A 1 | eg (base angles of) isosceles (triangle are equal) and (sum of) angles in a triangle (is 180) and (vertically) opposite angles |
| 20(a) | angle $BAD = 2x$ and (opposite angles of) cyclic quadrilateral (add to 180) | A1 | must see M1 |
| | Alternative method 2 Working ou | it angle <i>D</i> (| CF using angle at centre |
| | angle $DCF = 2x$ | M1 | |
| | angle at centre (is double angle at circumference) | A1 | |
| | Full method leading to angle $BAD = 2x$ and full reasoning for their method | A1 | must see M1 eg angle $BCD = 180 - 2x$ and angle $BAD = 2x$ and angles on a (straight) line (add to 180) and (opposite angles of) cyclic quadrilateral (add to 180) |

Mark scheme and Additional Guidance continue on the next three pages

| Q | Answer | Mark | Comments |
|---|--------|------|----------|
|---|--------|------|----------|

| | Alternative method 3 Working ou | t angle <i>D</i> | CF not using angle at centre |
|---------------|---|------------------|--|
| | Full method leading to angle $DCF = 2x$ | M1 | eg angle $CFE = x$ and angle $DCF = 2x$ |
| 20(a) cont | Full reasoning for their method | A1 | eg (base angles of) isosceles (triangle are equal) and exterior angle (of triangle is sum of interior opposite angles) |
| | Full method leading to angle $BAD = 2x$ and full reasoning for their method | A1 | must see M1 eg angle $BCD = 180 - 2x$ and angle $BAD = 2x$ and angles on a (straight) line (add to 180) and (opposite angles of) cyclic quadrilateral (add to 180) |

Mark scheme and Additional Guidance continue on the next two pages

| Q | Answer | Mark | Comments |
|---------------|--|------|---|
| | | | |
| | Alternative method 4 | | |
| | Full method leading to angle $DFC = 90 - x$ and angle $ABC = 90 - x$ | M1 | eg angle $CFE = x$ and angle $DFE = 90$ and angle $DFC = 90 - x$ and angle $CDF = 90 - x$ and angle $ADC = 90 + x$ and angle $ABC = 90 - x$ |
| 20(a) cont | Full reasoning for their method | A1 | eg (base angles of) isosceles (triangle are equal) and (angle in a) semicircle (is 90) and (sum of) angles in a triangle (is 180) and angles on a (straight) line (add to 180) and (opposite angles of) cyclic quadrilateral (add to 180) |
| | angle $BAD = 2x$ and (sum of) angles in a triangle (is 180) | A1 | must see M1 |

Additional Guidance is on the next page

| Q | Answer | Mark | Comments |
|---|--------|------|----------|
| | | | |

| | Additional Guidance | |
|---------------|---|--------|
| | It is possible to score M1A1A0 or M1A0A1 | |
| | Do not award any marks from angles on the diagram | |
| | Angles must be stated unambiguously eg condone angle <i>B</i> but do not condone angle <i>D</i> | |
| | 'angle' may be missing or replaced by a symbol - mark intention | |
| | angle CFE may be seen as angle EFC or angle BFE etc | |
| 20(5) | For (base angles of) isosceles (triangle are equal) allow radii (are equal) | |
| 20(a) cont | For (sum of) angles in a triangle (is 180) allow triangle is 180 | |
| | Use judgement when considering wording of reasons and allow abbreviations | |
| | Alt 2 Final A1 reason may be | |
| | exterior angle of cyclic quadrilateral (equals interior opposite angle) | |
| | Choose the scheme that favours the student | |
| | Ignore angles that are not needed for their scheme even if incorrect | |
| | Allow recovery of missing brackets | |
| | Starting with angle $BAD = 2x$ | M0A0A0 |

| Q | Answer | Mark | Comments |
|-------|---|------------------------|------------------------------------|
| | | | |
| | 30 | | B1 correct equation or calculation |
| | eç | eg $90 + 2x + x = 180$ | |
| | | B2 | or $90 - x = 2x$ |
| | | B2 | or $3x = 90$ |
| 20(b) | | | or $6x = 180$ |
| 20(5) | | | or 90 ÷ 3 |
| | Additional Guidance | | |
| | Ignore any expressions for angles and any other calculated angles | | |
| | Ignore any reasons | | |

| Q | Answer | Mark | Comments |
|----|--|------------|---|
| | | | |
| | $8^{2} + 12^{2}$ or $64 + 144$ or 208 or $8^{2} + 12^{2} + 15^{2}$ or $64 + 144 + 225$ or 433 | M1 | HC ² or CE ² implied by 2nd M1 |
| | $\sqrt{8^2 + 12^2}$ or $\sqrt{208}$ or $4\sqrt{13}$ or 14.4 or $\sqrt{8^2 + 12^2 + 15^2}$ or $\sqrt{433}$ or 20.8 | M1dep | oe may be on diagram fully correct trigonometry method leading to 14.4 or 20.8 can score M2 eg $8 \div \sin \left(\tan^{-1} \frac{8}{12} \right)$ or $8 \div \sin \left(\tan^{-1} \frac{8}{\sqrt{12^2 + 15^2}} \right)$ |
| 21 | $\tan x = \frac{15}{\sqrt{8^2 + 12^2}}$ or $\cos x = \frac{\sqrt{8^2 + 12^2}}{\sqrt{8^2 + 12^2 + 15^2}}$ or $\sin x = \frac{15}{\sqrt{8^2 + 12^2 + 15^2}}$ | M1dep | oe eg tan $x = [1.04, 1.042]$ or or $\cos x = [0.69, 0.6934]$ or $\sin x = [0.72, 0.7212]$ or $90 - \tan^{-1} \frac{\sqrt{8^2 + 12^2}}{15}$ dep on M2 any letter |
| | 46(.1) | A1 | |
| | Ad | ditional G | Guidance |
| | 3rd M1 If using sine rule or cosine rule, must be $eg \cos x = \frac{20.8^2 + 14.4^2 - 15^2}{2 \times 20.8 \times 14.4}$ (or | | orm $\cos x = \text{ or } \sin x =$ [0.69, 0.6934]) |
| | 3rd M1 Condone $\tan = \frac{15}{\sqrt{8^2 + 12^2}}$ e | МЗ | |
| | Allow the first 2 M marks even if not su | y used | |
| | Allow recovery of missing brackets | | |

| Q Answer Mark Comments | |
|------------------------|--|
|------------------------|--|

| | Alternative metho | od 1 | | |
|-------|--|--|-------|--|
| 22(a) | $2\sin^{2}x - 1 + 1 - \sin^{2}x$ or $2\sin^{2}x - (\sin^{2}x + \cos^{2}x)$ or $2\sin^{2}x - \sin^{2}x - \cos^{2}x$ or $\sin^{2}x - \cos^{2}x + \cos^{2}x$ or $1 + \sin^{2}x - 1$ | $\cos^2 x) + \cos^2 x$ $s^2 x + \cos^2 x$ | M1 | use of $\sin^2 x + \cos^2 x = 1$ in numerator ignore any denominator |
| | $\frac{\sin^2 x}{\sin x \cos x}$ with M1 seen | $\frac{\sin^2 x}{\tan x \cos^2 x}$ with M1 seen | M1dep | simplification to one step from $\frac{\sin x}{\cos x}$ or $\frac{\tan^2 x}{\tan x}$ |
| | $\frac{\sin x}{\cos x}$ and $\tan x$ with M2 seen | $\frac{\tan^2 x}{\tan x} \text{ and } \tan x$ with M2 seen | A1 | SC3 equates given expression to tan x and cross multiplies to show equivalence with full working shown |

Mark scheme and Additional Guidance continue on the next two pages

| Q | An | swer | Mark | Comments | |
|---------------|--|--|-------|--|--|
| | Alternative metho | od 2 | | | |
| | $2(1 - \cos^2 x) - 1 + \cos^2 x$ or $2 - 2\cos^2 x - 1 + \cos^2 x$ | | M1 | use of $\sin^2 x + \cos^2 x = 1$ in numerator ignore any denominator | |
| | $\frac{1-\cos^2 x}{\sin x \cos x}$ and $\frac{\sin^2 x}{\sin x \cos x}$ with M1 seen | $\frac{1-\cos^2 x}{\sin x \cos x}$ and $\frac{\sin^2 x}{\tan x \cos^2 x}$ with M1 seen | M1dep | simplification to one step from $\frac{\sin x}{\cos x}$ or simplification to one step from $\frac{\tan^2 x}{\tan x}$ | |
| 22(a) cont | $\frac{\sin x}{\cos x} \text{ and } \tan x$ with M2 seen | $\frac{\tan^2 x}{\tan x} \text{ and } \tan x$ with M2 seen | A1 | SC3 equates given expression to tan x and cross multiplies to show equivalence with full working shown | |
| | Alternative method 3 | | | | |
| | $\frac{2\sin x}{\cos x} - \frac{\sin^2 x}{\sin x \cos}$ | x | M1 | from $\frac{2\sin^2 x}{\sin x \cos x} - \frac{1 - \cos^2 x}{\sin x \cos x}$ | |
| | $2\tan x - \frac{\sin^2 x}{\sin x \cos x}$ | - x | | simplification to one step from $2\tan x - \tan x$ | |
| | or $ \frac{2\sin x}{\cos x} - \frac{\sin x}{\cos x} $ with M1 seen | | M1dep | | |
| | 2tan x - tan x and with M2 seen | tan x | A1 | SC3 equates given expression to tan x and cross multiplies to show equivalence with full working shown | |

Additional Guidance is on the next page

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| | Additional Guidance | | | | | |
|---------------|---|--------|--|--|--|--|
| | Equating given expression to $\tan x$ and cross multiplying can score SC3 or M1M0A0 | | | | | |
| | eg1 Alt 1 | | | | | |
| | $\frac{2\sin^2 x - 1 + \cos^2 x}{\sin x \cos x} = \tan x$ | | | | | |
| | $2\sin^2 x - 1 + \cos^2 x = \tan x \sin x \cos x$ | | | | | |
| | $2\sin^2 x - 1 + 1 - \sin^2 x = \tan x \sin x \cos x \qquad \text{(scores M1 here for LHS)}$ | M1M0A0 | | | | |
| 22(a) cont | $\frac{2\sin^2 x - 1 + \cos^2 x}{\sin x \cos x} = \tan x$ $2\sin^2 x - 1 + \cos^2 x = \tan x \sin x \cos x$ $2\sin^2 x - 1 + 1 - \sin^2 x = \tan x \sin x \cos x$ | | | | | |
| | $\sin^2 x = \tan x \sin x \cos x$ $\sin^2 x = \frac{\sin x}{\cos x} \sin x \cos x$ | 200 | | | | |
| | $\sin^2 x = \sin^2 x$ | SC3 | | | | |
| | Use of $\sin x = \frac{\text{opp}}{\text{hyp}}$ etc | M0M0A0 | | | | |
| | Allow sin or s for sin x etc | | | | | |
| | Condone $\sin x^2$ for $\sin^2 x$ etc | | | | | |
| | | | | | | |
| | Alts 1 and 2 | | | | | |
| | For A1 $\frac{\sin x}{\cos x}$ is implied by $\frac{\sin^2 x}{\sin x \cos x}$ with cancelling shown | | | | | |

| Q | Answer | Mark | Comments | ; | |
|-------|--|------|----------|----|--|
| | 135 and 315 with no other solutions [0, 360] B2 B1 135 with no other solution or 315 with no other solution SC1 135 and 315 with on solution [0, 360] Additional Guidance | | | | |
| | Mark the answer line unless blank | | ardarioo | | |
| | eg 135 and 315 in working with 135 on answer line | | | | |
| | -45 and 135 and 315 | | B2 | | |
| 22(b) | -45 and 135 | | | B1 | |
| | Ignore incorrect solutions outside the ra | B2 | | | |
| | 135 and 225 and 315 | | SC1 | | |
| | Both answers embedded ie tan 135 tan 315 | | | | |
| | 0 and 135 and 225 and 315 | | В0 | | |
| | 45 and 135 | | В0 | | |
| | 225 and 315 | | | | |

| | (1, -3) | B1 | | |
|-------|---------------------------------|----|--|----|
| 23(a) | 23(a) Additional Guidance | | | |
| | Mark intention eg condone 1, -3 | | | B1 |

| Q | Answer | Mark | Comments | i |
|-------|--|------------|-----------------------------------|-------------|
| | Alternative method 1 | | | |
| | $-3 + \sqrt{25}$ (= 2) or -3 + 5 (= 2) | B1 | oe eg 5 - 3 (= 2) or 2 + 3 | 3 = 5 |
| | Alternative method 2 | | | |
| | $(y + 3)^2 = 25$ and $y = 2$ or | | oe eg $(1-1)^2 + (y+3)^2 = 25$ | and $y = 2$ |
| 23(b) | y + 3 = 5 and $y = 2$ | B1 | | |
| | $(2+3)^2 = 25$ | | | |
| | Ad | ditional G | uidance | |
| | (1, -3) + (0, 5) = (1, 2) so $y = 2$ | | | В0 |
| | Allow -3 + radius of 5 | | | B1 |
| | 2 = 0x + c | | | |
| | c = 2 so $y = 2$ | | | В0 |

| Q | Answer | Mark | Comments | | | |
|-------|---|-------|---|--|--|--|
| | Alternative method 1 Using equation PR | | | | | |
| | $\frac{-7 - \text{their } -3}{4 - \text{their } 1} \text{or } -\frac{4}{3}$ | M1 | oe grad <i>PC</i> their –3 and their 1 from (a) | | | |
| | $-1 \div \text{their} -\frac{4}{3} \text{ or } \frac{3}{4}$ | M1 | oe grad PR their $-\frac{4}{3}$ must be a value | | | |
| | $27 = \text{their } \frac{3}{4}(x - 4)$ | | (gradient $PR = \frac{3}{4}$ is M2 oe equation PR with $y = 2$ substituted | | | |
| | 4` ′ | M1dep | eg $2 = \frac{3}{4}x - 10$ dep on 2nd M1 | | | |
| 23(c) | 16 | A1ft | only ft their -3 and their 1 from (a) | | | |
| | Alternative method 2 Using $RC^2 = CP^2 + PR^2$ or $PR^2 = QR^2$ with $R(x, 2)$ | | | | | |
| | $(x - \text{their 1})^2 + (2 - \text{their } - 3)^2$ = $(2 - \text{their } -3)^2 + (x - 4)^2 + (27)^2$ | M1 | oe eg $(x-1)^2 = (x-4)^2 + (2-7)^2$ their –3 and their 1 from (a) | | | |
| | $x^{2} - 2x + 1 + 25$ $= 25 + x^{2} - 8x + 16 + 81$ | M1dep | oe brackets expanded | | | |
| | 96 = 6x or $96 \div 6$ | M1dep | oe linear equation or calculation dep on M2 | | | |
| | 16 | A1ft | only ft their -3 and their 1 from (a) | | | |

Mark scheme and Additional Guidance continue on the next three pages

| Q | Answer | Mark | Comments | | | | |
|---------------|--|-------|---|--|--|--|--|
| | Alternative method 3 Using equation CR | | | | | | |
| | $\frac{-7-2}{4-\text{their 1}}$ or -3 | M1 | oe grad PQ their 1 from (a) | | | | |
| | $-1 \div \text{their} -3 \text{ or } \frac{1}{3}$ | M1 | oe grad CR their –3 must be a value (gradient $CR = \frac{1}{3}$ is M2 | | | | |
| | $2 - \text{their } -3 = \text{their } \frac{1}{3} (x - \text{their } 1)$ | M1dep | oe equation <i>CR</i> with $y = 2$ substituted eg $2 = \frac{1}{3}x - \frac{10}{3}$ dep on 2nd M1 | | | | |
| | 16 | A1ft | only ft their –3 and their 1 from (a) | | | | |
| 23(c) cont | Alternative method 4 Using equation MR where M is the midpoint of PQ | | | | | | |
| | $\frac{-7-2}{4-\text{their 1}}$ or -3 | M1 | oe grad <i>PQ</i> their 1 from (a) | | | | |
| | $-1 \div \text{their} -3 \text{ or } \frac{1}{3}$ | M1 | oe grad MR their –3 must be a value (gradient $MR = \frac{1}{3}$ is M2 | | | | |
| | $\left(\frac{4 + \text{their 1}}{2}, \frac{-7 + 2}{2}\right)$ or $(2.5, -2.5)$ and $2 - \text{their } -2.5 = \text{their } \frac{1}{3}(x - \text{their } 2.5)$ | M1dep | oe midpoint of PQ and equation MR with $y = 2$ substituted eg $2 = \frac{1}{3}x - \frac{10}{3}$ dep on 2nd M1 | | | | |
| | 16 | A1ft | only ft their 1 from (a) | | | | |
| | | | | | | | |

Mark scheme and Additional Guidance continue on the next two pages

| Q | Answer | Mark | Comments | | |
|-------|--|------------------|---|--|--|
| | Alternative method 5 Using equat | ion <i>MC</i> wh | ere <i>M</i> is the midpoint of <i>PQ</i> | | |
| | $\left(\frac{4 + \text{their 1}}{2}, \frac{-7 + 2}{2}\right)$ or $(2.5, -2.5)$ | M1 | oe midpoint of PQ their 1 from (a) | | |
| | $\frac{\text{their} - 3 - \text{their} - 2.5}{\text{their } 1 - \text{their } 2.5} \text{or} \frac{1}{3}$ | M1dep | oe grad MC | | |
| | 2 - their -3 = their $\frac{1}{3}(x - \text{their 1})$ or 2 - their -2.5 = their $\frac{1}{3}(x - \text{their 2.5})$ | M1dep | oe equation <i>MC</i> with $y = 2$ substituted eg $2 = \frac{1}{3}x - \frac{10}{3}$ dep on M2 | | |
| 23(c) | 16 | A1ft | only ft their -3 and their 1 from (a) | | |
| cont | Alternative method 6 Using trigonometry where M is the midpoint of PQ | | | | |
| | $(QM =) \frac{1}{2} \sqrt{(4 - \text{their 1})^2 + (-7 - 2)^2}$ or $\frac{1}{2} \sqrt{90}$ or 4.74 | M1 | | | |
| | $\sin^{-1}\left(\frac{\text{their 4.74}}{5}\right)$ or (angle QCM=) 71.5 or 71.6 | M1dep | oe angle <i>QCM</i> | | |
| | tan (their 71.5) = $\frac{x - \text{their 1}}{5}$ | M1dep | using triangle QCR | | |
| | 16 | A1ft | only ft their 1 from (a) | | |
| | | | | | |

Additional Guidance is on the next page

| Q | Answer | Mark | Comments | | | | |
|--|--|------|--------------------------------------|--|--|--|--|
| | Additional Guidance | | | | | | |
| | Allow (16,) to imply answer 16 Alt $1 - \frac{4}{3}x$ is M0 unless recovered | | | | | | |
| 23(c) | | | | | | | |
| cont | (a) (1, -2) | | | | | | |
| grad $PC = -\frac{5}{3}$ grad $PR = \frac{3}{5}$ | | | | | | | |
| | Answer 19 (3rd M1 can be implied by A1ft answer) M1A1 | | | | | | |
| | | | | | | | |
| | $3x^4$ or $4x^3$ | M1 | oe eg $5 \times \frac{3}{5} x^{5-1}$ | | | | |
| | $3x^4 + 4x^3$ | A1 | | | | | |
| | $x^{3}(3x + 4) (= 0)$ allow partial factorisation of their $3x^{4} + 4$ if at least x is taken as a factor | | | | | | |
| | | | ft their two terms if M1 scored | | | | |

24

 $x^3(3x + 4) (= 0)$

 $(x =) 0 \text{ and } (x =) -\frac{4}{3}$

with no other solutions

and

| Additional Guidance | | | | | |
|---|------------|----------------------|----------------------------|------|--|
| $3x^4 + 4x^3 = 0$ | | | | M1A1 | |
| $x = 0 \text{ and } x = -\frac{4}{3}$ | | | | M0A0 | |
| Condone $y = 3x^4 + 4x^3$ | | | | M1A1 | |
| Ignore higher derivatives | | | | | |
| Condone (0,) and $\left(-\frac{4}{3},\right)$ for $(x = \frac{1}{3})$ |) 0 and (a | $c =) -\frac{4}{3}$ | | | |
| Allow -1.33 for $-\frac{4}{3}$ (ignore any incompared in the second context). | rect conve | ersion attempt af | $(ter - \frac{4}{3} seen)$ | | |

Α1

allow partial factorisation if at least x is

taken as a factor

| Q | Answer | Mark | Comments | | |
|----|--------------------------------------|---------------------------------------|--|-----------|--|
| | | | | | |
| | Alternative method 1 | T | | | |
| | $(-c)^3 - 10(-c) - c (= 0)$ | | oe | | |
| | or $-c^3 + 10c - c = 0$ | M1 | | | |
| | or | IVII | | | |
| | $-c^3 + 9c (= 0)$ | | | | |
| | $c(9-c^2) (= 0)$ | | oe factorised expression or d | luadratic | |
| | or | | equation | | |
| | c(3+c)(3-c) (= 0) | M1dep | | | |
| | or | | | | |
| | $c^2 = 9$ | | | | |
| | 3 with no other value(s) | A1 | SC2 answer 3 with one or b –3 and 0 and no other value | oth of | |
| 25 | Alternative method 2 | | | | |
| | $(x+c)(x^2-cx-1)$ | M1 | | | |
| | $-1 - c^2 = -10$ | M1dep | oe quadratic equation | | |
| | 3 with no other value(s) | A1 | SC2 answer 3 with one or both of | | |
| | | Ai | -3 and 0 and no other value | | |
| | Additional Guidance | | | | |
| | $(-3)^3 - 10(-3) - 3 = 0$ and Answer | 3 (no pa | art marks) M2A1 | | |
| | $(-3)^3 - 10(-3)3 = 0$ and Answe | $(x)^3 - 10(-3) - 3 = 0$ and Answer 3 | | Zero | |
| | $3^3 - 10(3) - 3 = 0$ and Answer 3 | | | Zero | |
| | Answer 3 with no incorrect working | | | M2A1 | |
| | Allow recovery of missing brackets | | | | |

Comments

Mark

Q

Answer

| | | <u> </u> | | | |
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| | I | • | | | |
| | Alternative method 1 | | | | |
| | $(x+3)^2$ | M1 | | | |
| | $(x + 3)^2 - 3^2 - a$ or $(x + 3)^2 - 3^2 \ge a$ or $(x + 3)^2 \ge a + 3^2$ | M1dep | oe expression or inequality eg $(x + 3)^2 \ge 9 + a$ allow \ge to be any inequality symbol or = eg allow $(x + 3)^2 - 9 = a$ implies M2 | | |
| 26 | $-3^{2} - a \geqslant 0$ or $-3^{2} - a \geqslant 0$ | M1dep | oe inequality eg $-9 - a \ge 0$ or $-9 - a > 0$ or $a < -9$ implies M3 | | |
| | $a \leqslant -9 \text{ or } -9 \geqslant a$ | A1 | SC1 $x^2 + 6x - a \ge 0$ oe inequality (may be seen in working lines) | | |
| | Alternative method 2 | | | | |
| | 2x + 6 = 0 | M1 | must have = 0 | | |
| | (minimum at) $x = -3$ | M1dep | implies M2 $x = -3$ must be the only value or be clearly chosen | | |
| | $(-3)^2 + 6 \times (-3) - a \ge 0$ or $(-3)^2 + 6 \times (-3) - a > 0$ | M1dep | oe inequality eg $9-18-a\geqslant 0$ or $9-18-a>0$ or $a<-9$ implies M3 | | |
| | $a \leqslant -9$ or $-9 \geqslant a$ | A1 | SC1 $x^2 + 6x - a \ge 0$ oe inequality (may be seen in working lines) | | |

Mark scheme and Additional Guidance continue on the next page

| Q | Answer | Mark | Comments | |
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| | | | | |
| | Alternative method 3 | | | |
| | $6^2 - 4 \times 1 \times -a$ | | $b^2 - 4ac$ | |
| | | M1 | must be selected if seen in quadratic formula | |
| | $6^2 - 4 \times 1 \times -a \leqslant 0$ | | oe inequality | |
| | or | M1dep | implies M2 | |
| | $6^2 - 4 \times 1 \times -a < 0$ | | | |
| | 36 + 4 <i>a</i> ≤ 0 | | oe inequality eg $4a \leqslant -36$ | |
| 26 | or | M1dep | implies M3 | |
| cont | 36 + 4 <i>a</i> < 0 | | | |
| | $a \leqslant -9 \text{ or } -9 \geqslant a$ | A 4 | SC1 $x^2 + 6x - a \ge 0$ oe inequality | |
| | | A1 | (may be seen in working lines) | |
| | Additional Guidance | | | |
| | Alt 1 | | | |
| | 2nd M1 Any inequality symbol or = allowed | | | |
| | 3rd M1 Only the inequality symbols shown are allowed (do not allow =) | | | |
| | Allow $(x + 3)(x + 3)$ for $(x + 3)^2$ | | | |
| <u> </u> | | | | |

| Q | Answer | Mark | Comments | | |
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| | | | | | |
| | Alternative method 1 | | | | |
| 27 | Shows substitution of a value of $x < -2$ into $\frac{dy}{dx}$ and shows substitution of a value of $x > -2$ into $\frac{dy}{dx}$ | M1 | eg $(-3+2)^{6} + (-3+2)^{4}$ and $(-1+2)^{6} + (-1+2)^{4}$ allow $(-1)^{6} + (-1)^{4} \text{ with } x = -3 \text{ stated}$ and $(1)^{6} + (1)^{4} \text{ with } x = -1 \text{ stated}$ | | |
| | Evaluates both correctly or states that each is positive with M1 seen | M1dep | eg $(-3+2)^{6} + (-3+2)^{4} = 2$ and $(-1+2)^{6} + (-1+2)^{4} = 2$ allow $(-1)^{6} + (-1)^{4} = 2 \text{ with } x = -3 \text{ stated}$ and $(1)^{6} + (1)^{4} = 2 \text{ with } x = -1 \text{ stated}$ | | |
| | Statement with M2 seen | A1 | eg either side of $P \frac{dy}{dx} > 0$ with M2 seen SC2 states two values of x (one < -2 and one > -2) and shows the correct value of $\frac{dy}{dx}$ for each and makes a statement SC1 states two values of x (one < -2 and one > -2) and shows the correct value of $\frac{dy}{dx}$ for each | | |

Mark scheme and Additional Guidance continue on the next three pages

| Q | Answer | Mark | Comments |
|------------|----------------------------------|-------|---|
| | | | |
| 27 cont | Alternative method 2 | | |
| | $x < -2$ and $(-)^6 + (-)^4$ | | allow without brackets |
| | and | M1 | allow less than for < etc |
| | $x > -2$ and $(+)^6 + (+)^4$ | | |
| | $x < -2$ and $(-)^6 + (-)^4 > 0$ | | allow without brackets |
| | and | M1dep | allow = $+$ for > 0 |
| | $x > -2$ and $(+)^6 + (+)^4 > 0$ | | |
| | Statement with M2 seen | | eg either side of $P \frac{dy}{dx} > 0$ with M2 seen |
| | | A1 | SC2 states two values of x (one < -2 and one > -2) |
| | | | and shows the correct value of $\frac{dy}{dx}$ for |
| | | | each and makes a statement |
| | | | SC1 states two values of x (one < -2 and one > -2) |
| | | | and shows the correct value of $\frac{dy}{dx}$ for |
| | | | each |

Additional Guidance is on the next two pages

Comments

Mark

Answer

Q

Additional Guidance For A1 a clear statement is needed after M2 scored Examples of acceptable statements with M2 seen eg1 For x < -2 gradient is + and for x > -2 gradient is + eg2 To the left of P m > 0To the right of P m > 0eg3 (When both of their substitutions correctly evaluate to the same value) They are the same positive value eg4 Both gradients are the same sign eg5 m is + **both** times eg6 Gradient is **always** positive (apart from at *P*) eg7 **Function (or curve)** is increasing (either side of *P*) Allow a statement to be made using a diagram with M2 seen eg accept for eg2 above m > 0m > 0Allow a statement to be made using a table with M2 seen eg accept for eg1 above -3 -2 **-1** 0 + + When both of their substitutions correctly evaluate to the same positive value condone for the statement with M2 seen Gradients are the same (implies both positive) Do not accept for the statement eg1 Gradient is increasing eg2 m is positive eg3 Gradient is positive eg4 P is a point of inflection

Additional Guidance continues on the next page

| Q | Answer | Mark | Comments | | | |
|------------|---|-------------|----------|----|--|--|
| | | | | | | |
| 27 cont | Additional Guidance | | | | | |
| | Allow gradient or m for $\frac{dy}{dx}$ | | | | | |
| | For evaluations allow rounding or trunc | f or better | | | | |
| | Ignore higher derivatives | | | | | |
| | Ignore substitution of $x = -2$ | | | | | |
| | x = -3 gradient = 2 x = -1 gradient = 2 | | SC | 2 | | |
| | either side of <i>P</i> gradient > 0 | | | | | |
| | -3 -2 -1 2 0 2 gradient is positive | both times | SC | ;2 | | |
| | -3 -2 -1 2 0 2 | | SC | ;1 | | |