AQA Level 2 Further Mathematics Coordinate integral geometry



Section 1: Straight lines

Exercise

- 1. (a) For the points A(3, 1) and B(7, 4) calculate
 - (i) the gradient of AB
 - (ii) the gradient of a line perpendicular to AB
 - (iii) the midpoint of AB
 - (iv) the distance AB
 - (v) the coordinates of the point C which divides AB in the ratio 3:2.
 - (b) Repeat part (a) for the points A(-2, 9) and B(3, -1).
- 2. For the points P(2, -1) and Q(-4, 8), find
 - (i) the midpoint M of PQ
 - (ii) the coordinates of the point R such that PR:QR is 1:3
 - (iii) the coordinates of the point S such that PS:QS is 7:3.
- 3. Given the points A(3, 1), B(6, y) and C(12, -2) find the value(s) of y for which
 - (i) the line AB has gradient 2
 - (ii) the distance AB is 5
 - (iii) A, B and C are collinear
 - (iv) AB is perpendicular to BC
 - (v) the lengths AB and BC are equal
- 4. P is the point (2, 1), Q is (6, 9) and R is (10, 2).
 - Sketch the triangle PQR.
 - (ii) Prove that triangle PQR is isosceles.
 - (iii) Work out the area of triangle ABC.
- 5. The point E is (2, -1), F is (1, 3), G is (3, 5) and H is (4, 1). Show, by calculation, that EFGH is a parallelogram.
- 6. Find the equations of the following lines.
 - (i) parallel to y = 4x 1 and passing through (2, 3)
 - (ii) perpendicular to y = 2x + 7 and passing through (1, 2)
 - (iii) parallel to 3y + x = 10 and passing through (4, -1)
 - (iv) perpendicular to 3x + 4y = 12 and passing through (-3, 0)
 - (v) parallel to x+5y+8=0 and passing through (-1, -6)
- 7. Find the equation of the perpendicular bisector of AB in each of the following cases.
 - (i) A(1, 6), B(3, 2)
- (ii) A(8, -1), B(-2, 3)
- (iii) A(-5, 2), B(7, -4)
- (iv) A(-3, -5), B(5, 1)
- 8. A triangle has vertices E(2, 5), F(4, 1) and G(-2, -3).
 - Find the midpoint of each side and hence find the equations of the three medians. (Medians are the lines from the midpoint of each side to the opposite vertex).
 - (ii) Show that the point $(\frac{4}{3},1)$ lies on each median.

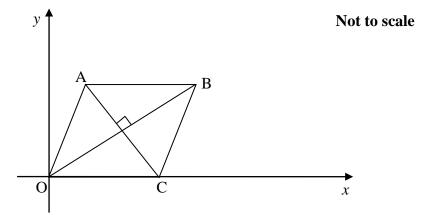


1 of 2 11/06/13 © MEI

AQA FM Coordinate geometry 1 Exercise

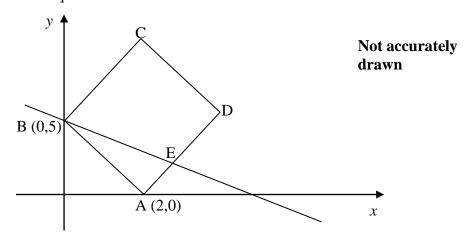
- 9. ABCD is a parallelogram. The equation of AB is y = 4x 3 and the equation of BC is y = 2x + 1.
 - (i) Find the coordinates of B.
 - (ii) The coordinates of A are (3, 9). Find the equation of AD.
 - (iii) The coordinates of C are (7, 15). Find the equation of CD.
 - (iv) Find the coordinates of D.
- 10. The diagram shows a rhombus OABD. O is the origin.

B is the point with coordinates (6, 4). D lies on the *x*-axis.



Find the coordinates of point A.

11. ABCD is a square. Point E cuts AD in the ratio 1:2.



Find the coordinates of the point where line BE crosses the *x*-axis.

2 of 2